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## The ICA-based Factor Decomposition of the Eurozone Sovereign CDS Spreads

Frank J. Fabozzi\*, Rosella Giacometti\*\*, and Naoshi Tsuchida\*\*\*

### Abstract

In this paper, we examine the factors driving Eurozone sovereign credit default swap (CDS) spreads during the Eurozone sovereign debt crisis. For identifying factors we utilize independent component analysis (ICA), a technique similar to principal component analysis (PCA). We identify three factors that impact spreads and capture the features specific to the crisis such as the breakup risk of the Eurozone: peripheral factor, global factor, and Eurozone common factor. In contrast, when PCA is applied, only a single factor is identified. Moreover, using ICA with a GARCH model, we show that the source of volatility for CDS spreads shifted from the global factor in 2009 and the peripheral factor in 2010 to the Eurozone common factor in 2012, and that the dynamic correlation reflects the decoupling between low credit countries such as Germany and high credit countries such as Greece. We also show that the goodness-of-fit of the ICA-based model is better than other models used such as the Student- $t$  copula model.

**Keywords:** independent component analysis (ICA); credit default swap (CDS); Eurozone sovereign debt crisis; redenomination risk

**JEL classification:** C18, G01, G15

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# 1 Introduction

The *Eurozone sovereign debt crisis* is an ongoing crisis. The crisis is said to have started in late 2009, and remains a critical sector of the global credit market where there is concern about sovereign risk. Prior to the crisis the credit risk of Eurozone countries was considered to be very low; however, after the onset of the crisis, the credit risk, as indicated by the widening of credit default swap (CDS) spreads and bond yields, has increased dramatically. Moreover, the credit spreads between countries with lower risk, such as Germany, and those with higher risk, such as Greece, widened substantially.

In this paper, we investigate the factors driving Eurozone sovereign CDS spreads. While a default of a country ultimately depends on reasons specific to the country, preceding studies reported that sovereign CDS spreads exhibit co-movements across countries. Using principal component analysis (PCA), Longstaff et al. (2011) studied the spreads of 26 sovereign CDSs of monthly frequency from 2000 to 2010. They reported that co-movements are linked to US equity, equity volatility, and bond risk premium. Pan and Singleton (2008) studied the term structure of three countries (Korea, Mexico, and Turkey) seeking to estimate default and recovery rates. They propose a pricing model with stochastic default intensity, and decompose the variation of CDS into default intensity and risk premium. The risk premium is shown to have co-movements across countries, and are linked to the CBOE VIX volatility index, US corporate bond spreads, and the volatility of the country's foreign exchange rate. Ang and Longstaff (2013) studied systemic credit shock by comparing the US and the Eurozone using the CDS for US Treasuries, US states, and major Eurozone countries. In the pricing model, they proposed the use of two types of credit events, systemic and sovereign-specific. They found that the systemic risk component is more important in the Eurozone than in the US, and is related to global financial factors such as the VIX index.

In addition to the issue of co-movements of CDS spreads, we consider two issues

specific to the the period which is referred to as the Eurozone sovereign debt crisis. First, during this a strong relation was observed between sovereign CDS spreads and the stability of the Eurozone financial sector. According to Mody (2009), following the US government bail out of Bear Stearns in 2008 the Eurozone sovereign CDS spread began widening, reflecting the rescuing cost of stressed financial institutions. Since the onset of the US subprime mortgage crisis starting in 2007, banks and other financial institutions have encountered difficulties, some being forced into bankruptcy while others being fortunate to be bailed out by governments. The costs of such government bailouts were potential so large that they were expected to increase the government debt level, resulting in increased sovereign credit risk. This is particularly the case in the Eurozone since the scale of the financial sector is larger than the other countries.<sup>1</sup> Considerable theoretical and empirical research has been devoted to show the fundamental relation between sovereign credit and the financial industry. One recent example of such research is the paper by Acharya et al. (2014).

The other issue of the Eurozone sovereign debt crisis we investigate is what is referred to as the “risk of convertibility” or the “risk of redenomination.” The President of the European Central Bank (ECB) Mario Draghi mentioned in a speech on July 26, 2012 that convertibility risk was charged on the Eurozone sovereign CDS spreads (Draghi, 2012). Before this speech, the crisis of the Eurozone became deepened, and the CDS spreads of countries such as Italy, Portugal and Spain increased to the level such that market participants started thinking of the possible breakup of the Eurozone into national currencies. President Draghi stated that “the euro is irreversible,” and confirmed that the ECB would take whatever the action was in order to preserve the Eurozone. The word redenomination risk is also used in referring to this kind of risk (Draghi and Constâncio,

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<sup>1</sup>According to Table 2.3.1 in the report about the EU banking sector published by European Commission (2012), the ratio of the bank assets over GDP is 349% in the EU, 78% in the US, and 174% in Japan.

2012). De Santis (2015) showed that the redenomination risk serves as the systemic risk during the crisis period; Krishnamurthy et al. (2013) showed that it is to some extent through the reduction of redenomination risk that some monetary measures by the ECB (such as the Outright Monetary Transaction) works effectively during the Eurozone sovereign crisis.

As a consequence of this crisis, the decoupling of sovereign credits across the Eurozone countries was observed, as well as the co-movements of the sovereign credits. The countries with low credit risk such as Germany are often colloquially termed *core* countries, whereas those with high credit risk countries such as Greece termed *peripheral* countries. There are some who question whether these terms are appropriate (Kaletsky, 2012). However, these terms are commonly used, appearing in some prior studies about the Eurozone (e.g., Artis and Zhang, 2001; Stockhammer, 2011). We use these terms since we consider it is important to investigate the decoupling between the “core” countries and “peripheral” countries.

In this paper, our objective is to identify the factors driving the changes in CDS spreads, separating the decoupling factor and the co-movement factor. Following Kumiega et al. (2011) and García-Ferrer et al. (2012), in this paper we employ independent component analysis (ICA) for that purpose. Although similar to factor analysis (FA) and PCA in that it is a linear model, ICA differs from these two traditional models in that its objective is to find a linear representation for non-Gaussian variables so that the components identified are statistically independent from the other components identified.<sup>2</sup>

The non-Gaussianity plays an essential role in ICA. If the data obey the Gaussian distribution, then ICA produces the same components as PCA. In the case of asset returns for financial instruments, there is a preponderance of empirical evidence that asset returns

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<sup>2</sup>The theory and applications of ICA and algorithms for solving for the components are described in Hyvärinen and Oja (2000) and Hyvärinen et al. (2001). Recent advances in ICA are described in Hyvärinen (2013).

violate the Gaussian assumption; for example, see Chapter 11 of Rachev et al. (2005). In fact, tail heaviness is the important feature of asset returns causing the catastrophic events realized in the financial market that began in 2007, as well as other documented market crashes (for example, see Kim et al., 2011). Consequently, the application of ICA to the analysis of asset returns seems to be more appropriate than other techniques that assume a Gaussian distribution.<sup>3</sup>

The paper is structured as follows. Section 2 briefly reviews the Eurozone sovereign CDS market during the crisis and describes the data we analyze. In Section 3 we discuss factor decomposition based on ICA and comparing the ICA results with those found using PCA. Section 4 discusses the volatility of the ICs and the correlation between the CDS spreads based on the GARCH model, and compares the goodness-of-fit of the ICA-based model with the alternative models using copula functions. Section 5 provides our conclusions.

## 2 The data and the Eurozone sovereign CDS market during the crisis

In this paper, we analyze Eurozone sovereign CDS spreads from January 2009 to December 2013 (see Figure 1).<sup>4</sup> More precisely, we use data for CDS spreads denominated in US dollars with a maturity of five years obtained from Bloomberg. We use weekly data to avoid noise that may be contained in daily data. The observation period is January

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<sup>3</sup>For example, Chapter 24 of Hyvärinen et al. (2001) shows several examples of ICA applications to financial data.

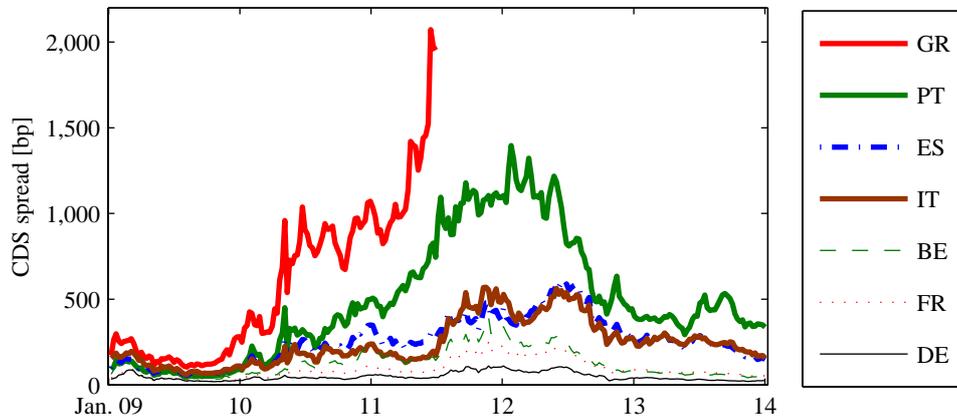
<sup>4</sup>Note that another source representing the sovereign credit is the yield of sovereign bonds. The CDS spread referencing an entity theoretically matches the spread of the bond yield issued by the entity over the risk free rate. In the real-world of financial markets, however, the market for these two credit products are very similar but not identical, reflecting the difference of some market features. For the Eurozone sovereign credit markets, Fontana and Scheicher (2010) showed that the difference between the CDS and cash bond markets arises because the cash market is less liquid than the CDS market, that is, the CDS market is more liquid. In this paper, therefore, we focus on the CDS spread.

2009 to December 2013. We use the CDS spreads of seven Eurozone countries: Belgium (BE), France (FR), Germany (DE), Greece (GR), Italy (IT), Portugal (PT), and Spain (ES). These countries account for more than 80% of the Eurozone GDP, and include the countries that attracted increased attention during the crisis.

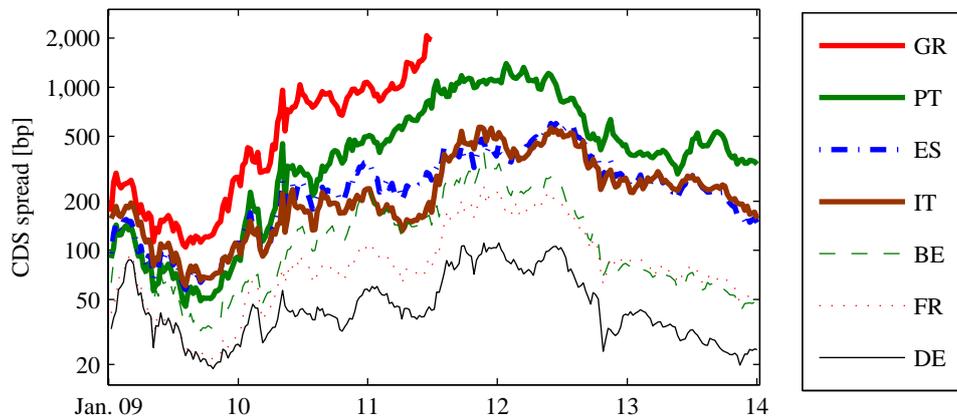
From Figure 1, we can observe that CDS spreads started widening from the middle of 2009, soared toward the middle of 2012, and then decreased. It is also observed that the level of the CDS spreads in 2013 is generally much higher compared to the level in the middle of 2009. Moreover, the difference of CDS spreads between the Eurozone sovereign countries in 2013 is much larger than that in 2009. Figure 1(b) shows the CDS spreads in logarithmic scale, depicting this credit decoupling more clearly.

The period depicted in Figure 1 contains the major part of what is referred to as the Eurozone sovereign debt crisis. The onset of the crisis is not precisely defined, but is usually considered as the end of 2009, in which bad news about sovereign debt were reported and their CDS spreads started widening. For example, on November 5, 2009, Reuters reported that the budget deficit of Greece was more than the double of what was previously announced. This news increased the Greek CDS spread.

Figure 1 shows that the Greek CDS spread skyrocketed toward the summer of 2011. Since its economy and fiscal conditions are one of the most fragile among the Eurozone, the country has attracted attention from market participants. On May 2, 2010, in exchange for a bailout loan amounting to € 110 billion, the Greek government agreed about its austerity program with the ECB, the European Commission (EC), and the International Monetary Fund (IMF). However, its CDS spread increased during the week of May 3 to 7, from 722 basis points (at the closing on April 30, the end of the last week) to 965 basis points (at the closing on May 7). On May 10, the spread dropped to 590 basis points, reportedly because of the introduction of the Security Market Programme by the ECB on that day (European Central Bank, 2010). However, it kept increasing after that



(a) Linear scale



(b) Log scale

Figure 1: CDS spreads of the seven Eurozone countries: Belgium (BE), France (FR), Germany (DE), Greece (GE), Italy (IT), Portugal (PT), and Spain (ES). The denomination currency is the US dollar, and the maturity is five years. Note that in the legend of the figure, the countries are in the descending order of the average values of CDS spreads. The data for Greece were discontinued in July 2011.

day. Finally, the International Swaps and Derivatives Association (ISDA) announced its resolution on March 9, 2012, that a restructuring credit event had occurred for the CDS contract referencing Greece (the Hellenic Republic; The International Swaps and Derivatives Association, 2012)

Obviously, Greece is the country we are most interested in. However, as already noted, the Greek CDS experienced a credit event, so it seems better to limit the data for Greece to the pre-2012 time period. On the other hand, we are also interested in investigating the CDS market around 2012, since the spreads for the other countries hit their maxima around that time. For these reasons, we partition the data into two parts. One part consists of all seven countries, covering the period from January 2009 to June 2011. The other part consists of all countries except Greece, covering the period from January 2009 to December 2013. We will refer to the former data as the “seven countries” data and the latter as the “six countries” data. The number of observations is 130 in the seven countries data and 261 in the six countries data.

Since we are interested in factors driving CDS spreads, we mainly focuses on the changes of CDS spreads, not on the levels. However, their scales are very different across the countries in our study. In order to adjust for this scale difference, we use the changes of logarithm (log-returns) of CDS spreads. Figure 1(b) suggests that the logarithm of CDS spreads is closer to the usual Brownian motion than the CDS spreads themselves are. From the Table 1 which provides descriptive statistics of the log-returns of CDS spreads, it can be seen that the standard deviations of log-returns are about the same (ranging from 10% to 15%) across the countries. This justifies the use of log-returns for comparison across the countries. Taking logarithm generally decreases the tail heaviness of the given data, but the values of kurtosis in Table 1 indicate that the log-returns of CDS spreads exhibit tail heaviness in this case.

Table 1: Descriptive statistics of log-returns of sovereign CDS spreads, their principal components (PCs), and their independent components (ICs). Columns “avg.,” and “std.,” show average and standard deviation, whose unit is 1% for the log-returns of CDS spreads (for the scales of the PCs and ICs, see Table 3). Column “skew.” shows skewness. Column “kurt.” shows kurtosis (not excess kurtosis; that is, 3.0 if the variable obeys the Gaussian distribution).

	<b>Seven countries from January 2009 to June 2011 (130 datapoints)</b>				<b>Six countries from January 2009 to December 2013 (261 datapoints)</b>			
	<b>avg.</b>	<b>std.</b>	<b>skew.</b>	<b>kurt.</b>	<b>avg.</b>	<b>std.</b>	<b>skew.</b>	<b>kurt.</b>
Logarithmic returns of CDS spreads								
Belgium	0.63	11.54	0.13	3.95	-0.13	10.11	0.07	4.47
France	0.28	11.50	-0.31	4.01	-0.02	10.12	-0.29	4.44
Germany	-0.07	11.53	-0.42	4.75	-0.25	10.42	-0.45	5.47
Greece	1.65	13.52	-0.28	6.09				
Italy	0.00	12.31	-0.43	6.11	-0.03	10.75	-0.32	6.26
Portugal	1.61	14.97	-0.92	10.31	0.50	11.94	-0.70	12.63
Spain	0.77	12.53	-0.55	6.17	0.15	10.54	-0.48	6.74
Principal components (PCs)								
PC1	0	2.34	-0.55	4.70	0	2.14	-0.43	5.07
PC2	0	0.82	1.52	9.15	0	0.86	0.68	9.77
PC3	0	0.54	-0.86	4.84	0	0.51	-0.25	4.88
Independent components (ICs)								
IC1	0	1	-1.52	21.02	0	1	-1.76	15.20
IC2	0	1	-0.01	7.54	0	1	-0.54	8.19
IC3	0	1	0.04	3.99	0	1	0.28	3.28

### 3 Factor Decomposition of CDS based on ICA

In this section, we discuss factor decomposition of the data we presented in Section 2. For that purpose, we introduce the idea of ICA, and present the model based on that in Section 3.1.

#### 3.1 The return model based on ICA and PCA

Suppose a  $q$ -dimensional random vector  $\mathbf{X} = (X_1, \dots, X_q)^\top$  representing the observable variables, and assume  $E[\mathbf{X}] = 0$ . ICA is the following model of  $\mathbf{X}$ :

$$\mathbf{X} = \mathbf{A}\mathbf{S}, \tag{1}$$

where  $\mathbf{S} = (S_1, \dots, S_q)^\top$  is a set of  $q$  independent random variables and  $A$  is a  $q$ -by- $q$  constant matrix. The random variable  $S_j$ ,  $j = 1, \dots, q$ , is referred to as the *independent component* (IC). The independence is equivalent to the following equation about the probability density function (PDF):

$$f_{\mathbf{S}}(s) = f_{S_1}(s_1) \cdots f_{S_q}(s_q), \tag{2}$$

where  $s = (s_1, \dots, s_q)^\top$  is a possible value of  $\mathbf{S}$  and  $f_{\mathbf{S}}$  and  $f_{S_j}$  are the joint and the marginal PDF of  $\mathbf{S}$  and  $S_j$ , respectively.

An algorithm for ICA decomposes  $\mathbf{X}$  into  $\mathbf{S}$  by finding the matrix  $A$  such that  $S_j$  is as *independent* from the other  $S_{j' \neq j}$  as possible.<sup>5</sup> There are several algorithms for finding  $A$ ; among them, the *fastICA* algorithm introduced by Hyvärinen and Oja (2000) realizes

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<sup>5</sup>Note that the components obtained by an ICA algorithm are not completely independent of each other. For example, if each component of  $\mathbf{X}$  is completely dependent on each other, such decomposition is impossible. However, practically, we apply ICA to the non-correlated data obtained by PCA, as discussed later. While no correlation does not mean independence, it is close to independence. Therefore we postulate that each component obtained using ICA is independent.

ICA by maximizing the non-Gaussianity of each independent component based on the fixed point method.

Equation (1) has the same form as PCA. Although PCA and ICA provide for linear transformation of multidimensional data, they differ as to how to determine the matrix  $A$ . PCA diagonalizes the covariance matrix of  $\mathbf{X}$  in equation (1) by a unitary matrix  $A$ , usually denoted as  $U$ , that is,

$$\left\{ \begin{array}{l} \mathbf{X} = U\mathbf{P}, \\ \text{cov}\mathbf{X} = UDU^\top, \\ D = \text{cov}\mathbf{P} = \text{diag}(\lambda_1, \dots, \lambda_q), \\ UU^\top = U^\top U = I_q, \end{array} \right. \quad (3)$$

where  $\mathbf{P} = (P_1, \dots, P_q)^\top$ . As a result,  $P_j$  in PCA has no correlation with the other  $P_{j'}$ .  $P_j$  is referred to as the *principal component* (PC), and its variance is equal to the diagonal element  $\lambda_j$ . Conventionally,  $\lambda_j$  is in the descending order as  $\lambda_1 \geq \dots \geq \lambda_q \geq 0$ , and  $P_1$  is referred to as the first PC since its variance is the largest.

ICA is often used in combination with PCA. ICA cannot determine the scales of the ICs, since  $A$  can be a non-unitary matrix. Consequently, ICA cannot reduce the dimension of data based on their scales. In contrast, PCA can reduce the data dimension based on the variances of the PCs, since the variances are determined with the unitarity of  $U$ . Therefore, for the data with large dimension  $d$  ( $> q$ ), the dimension is reduced from  $d$  to  $q$  by PCA at first, and then ICA is applied to the  $q$ -dimensional data obtained by PCA.

Our principal interest is applying ICA to the multivariate time series of the CDS spreads. Let  $\mathbf{r}_t = (r_{1t}, \dots, r_{dt})^\top$ ,  $t = 1, \dots, T$  denote the log-return of  $d$  sovereign CDS spreads on day  $t$ . Let us assume that the returns  $\mathbf{r}_t$  obeys a factor model with  $q$  ( $\leq d$ )

factors:

$$\left\{ \begin{array}{l} \mathbf{r}_t = \mu + A\mathbf{s}_t + \epsilon_t, \\ \mathbf{s}_t = (s_{1t}, \dots, s_{qt})^\top: \text{source of variation,} \\ \epsilon_t = (\epsilon_{1t}, \dots, \epsilon_{dt})^\top: \text{noise term,} \\ \mu: \text{constant vector, and} \\ A: d \times q\text{-constant matrix.} \end{array} \right. \quad (4)$$

Note that  $\mathbf{s}_t$  and  $\epsilon_t$  can be interpreted as the sources of variation of the CDS spreads and the noise term, respectively. We assume that these vectors are independent of each other.

We employ both PCA (PCA only) and ICA (ICA combined with PCA) to determine the matrix  $A$  and the series  $\{s_{jt}\}_{1 \leq t \leq T}$ ,  $j = 1, \dots, q$ , in equation (4). We use PCA for the correlation matrix, that is,  $X = D_r^{-1/2}(\mathbf{r}_t - \mu)$  in equation (3) where  $D_r = \text{diag}((\sigma_1^{(r)})^2, \dots, (\sigma_d^{(r)})^2)$  and  $\sigma_{jt}^{(r)} = \text{std}(r_{jt})$ . For ICA, we use the fastICA algorithm.<sup>6</sup>

We can derive the following formulae:

$$\mathbf{s}_t = (D_r^{-1/2}A)^+ D_r^{-1/2}(\mathbf{r}_t - \mu), \quad (5)$$

$$\epsilon_t = D_r^{1/2}U_b \mathbf{p}_t^b, \quad (6)$$

where  $X^+ = (X^\top X)^{-1}X^\top$ , which is the Moore-Penrose pseudoinverse for a matrix such that  $(X^\top X)$  is invertible,  $U_b$  is the right  $(d - q)$  columns of  $U$  in equation (3) and  $\mathbf{p}_t^b = (p_{q+1,t}, \dots, p_{dt})^\top$  is the PCs from the  $(q + 1)$  th to  $d$ th in equation (3).

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<sup>6</sup>We use the MATLAB code distributed by the authors at their webpage:

<http://www.cs.helsinki.fi/u/ahyvarin/> .

In the fastICA algorithm, we select the hyperbolic tangent (tanh) function as the nonlinearity function, and set the scale parameter as unity.

Table 2: The explanatory powers of the first three PCs and ICs. The table includes the results for two different data: the “Seven countries” data, from January 2009 to June 2011 including Greece, and the “Six countries” data, from January 2009 to December 2013 excluding Greece.

	PCA Results			ICA Results		
	PC1	PC2	PC3	IC1	IC2	IC3
Seven countries	78%	10%	4%	29%	26%	37%
Six countries	76%	12%	4%	29%	26%	38%

### 3.2 Decomposition results

Table 2 shows the “explanatory powers” of the first three PCs and ICs.<sup>7</sup> PC1, PC2 and PC3 in the table are the first, second, and the third PCs. IC1, IC2 and IC3 in the table are the ICs when we set  $q = 3$ .<sup>8</sup> The ICs are in the descending order of non-Gaussianity.

It can be seen from Table 2 that the explanatory powers of the first PC is 78% or 76%, which is dominant over the other two PCs which have much less explanatory powers. In stark contrast to the PC for PCA, the first three ICs when ICA is used have similar values of explanatory powers.

Table 3 shows the entries of the constant matrix  $A$  in equation (4) for both PCA and ICA, where the unit is one percent point per unit value of the PC or the IC. The  $R^2$  values of the regression for each factor for each country is also shown in the parentheses in the table. For example, PC1 in the seven countries data explains 77% of the CDS spread return of Belgium, and the CDS of Belgium increases by 4.32% when PC1 increases by

<sup>7</sup>Here, the explanatory power is defined in the following way: For each country and each component, a simple regression is estimated by setting the CDS spread returns of the country as the explained variable and the component as the explanatory variable, and obtain the coefficient of determination  $R^2$ . The explanatory power of the component is defined as the average of the  $R^2$  across the countries. Note that for PCA, the explanatory power by this definition matches its usual definition; that is, it is the ratio of the eigenvalue corresponding to the component over the total of the eigenvalues.

<sup>8</sup>Since the three ICs are linear transformations of the three PCs, the sum of the explanatory powers of the three PCs matches that of the three ICs.

Table 3: The factor loadings of the first three PCs and ICs. The unit of factor loadings is 1% increase of CDS spreads per one point increase of each PC or IC. The figures in parentheses are the  $R^2$  values of the regression for each component on each country. The parenthesized figures in the “Tot.” rows show the explanatory powers shown in Table 2.

	PCA Results			ICA Results		
	PC1	PC2	PC3	IC1	IC2	IC3
Seven countries from January 2009 to June 2011						
Tot.	(78%)	(10%)	(4%)	(29%)	(26%)	(37%)
BE	4.32 (77%)	2.19 (2%)	-6.92 (10%)	2.91 (6%)	3.93 (12%)	9.70 (71%)
FR	4.28 (76%)	5.58 (16%)	2.92 (2%)	2.09 (3%)	8.81 (59%)	6.40 (31%)
DE	4.10 (69%)	6.93 (25%)	1.06 (0%)	0.70 (0%)	8.58 (56%)	7.04 (38%)
GR	5.00 (75%)	-3.59 (5%)	9.24 (13%)	9.93 (54%)	7.56 (32%)	3.62 (7%)
IT	4.76 (82%)	-3.52 (6%)	-3.42 (2%)	7.71 (40%)	2.99 (6%)	8.12 (44%)
PT	5.79 (82%)	-5.09 (8%)	0.39 (0%)	10.58 (50%)	4.82 (10%)	8.00 (29%)
ES	5.00 (87%)	-3.93 (7%)	-1.84 (1%)	8.52 (47%)	3.64 (8%)	7.82 (39%)
Six countries from January 2009 to December 2013						
Tot.	(76%)	(12%)	(4%)	(29%)	(26%)	(38%)
BE	4.22 (80%)	2.03 (3%)	-5.25 (7%)	2.33 (5%)	4.28 (18%)	8.22 (66%)
FR	4.22 (80%)	3.99 (11%)	1.78 (1%)	2.78 (8%)	7.31 (52%)	5.71 (32%)
DE	3.98 (67%)	6.09 (25%)	3.14 (2%)	1.54 (2%)	8.67 (69%)	4.94 (23%)
IT	4.51 (80%)	-3.45 (8%)	-3.23 (2%)	6.47 (36%)	1.83 (3%)	7.67 (51%)
PT	4.60 (68%)	-5.76 (17%)	8.07 (12%)	10.62 (79%)	3.51 (9%)	3.54 (9%)
ES	4.48 (83%)	-3.75 (9%)	-2.62 (2%)	6.76 (41%)	1.78 (3%)	7.39 (49%)

one.

For PC1, the factor loadings range from 3.98 to 5.00, and the explanatory powers range from 67% to 87%. This PCA result suggests that PC1 can be considered as the common factor whose changes affect all the countries. In contrast, PC2 has much less value in terms of its explanatory power. Looking more closely at the PCA results, we see that the factor loadings for PC2 are positive for Belgium, France, and Germany, but negative for the other countries. The three countries for which the PC2 is positive are considered as the core countries, while the other countries are considered as the peripheral countries. From these observations, it can be argued that PC2 may be related to the difference between core countries and peripheral countries, while the difference explained by PC2 is much smaller than the common factor explained by PC1 from the viewpoint of explanatory power. As for PC3, it is difficult to find some tendency or interpretation.

As seen here, PCA has the advantage that it can reduce the dimension of data into the minimum number of factors needed to explain the data. The large value for the  $R^2$  of PC1 suggests that only PC1 should be considered and the other PCs can be ignored. However, decoupling of the credit spreads suggests adding an additional component in order to explain the decoupling. PC2 can be a candidate for such a component, and the values of factor loading reported in Table 3 show that to some extent PC2 fulfills that role. However, the small  $R^2$  values of PC2 show the difficulty of such interpretation. Therefore, we apply an alternative method of decomposition, ICA.

Turning to the results for the factor loadings obtained from ICA, we see that the factor loading for IC3 for all but Greece in the seven country data and Portugal in the six country data ranges from 4.94 to 9.70. For Greece in the seven country data, IC3's factor loading is 3.62, and for Portugal in the six country data, IC3's factor loading is 3.54. The explanatory powers of IC3 range from 23% to 71% for all countries except these two cases. For Greece in the seven countries, it is 7%, and for Portugal in the six countries, it is 9%. These ICA results suggest that IC3 is related to the changes of all countries except these two cases. Therefore it seems that IC3 can be viewed as the common factor.

The other two components, IC1 and IC2, have different characteristics. IC1 and IC2 have large factor loadings and explanatory powers for peripheral countries and core countries, respectively. Like PC2, IC1 and IC2 are related to the distinctive country groups in the Eurozone. However, different from PCA, ICA can separate the factor found by PC2 into the two factors reflecting the characteristics of the two country groups. Moreover, the explanatory powers of IC1 and IC2 are much larger than those of PC2, showing the significance of the factors.

These results show the relative advantage of ICA. ICA can find different multiple factors and these independent factors have an interesting interpretation concerning credit decoupling between countries. In addition, the role of the ICA-obtained factors are

comparable with respect to explanatory power, whereas the second and the third factors obtained from PCA are negligible compared to the first PC. However, in order to identify the ICs as meaningful factors, additional evidence would be required. For this purpose, we consider the relation of the ICs with the variables observed in the financial markets in Sections 3.3 and 3.4.

The descriptive statistics of the PCs and the ICs are shown in Table 1. The PCs are in the descending order of their standard deviation values. In contrast, the ICs are in the descending order of their kurtosis values, since ICs are obtained by maximizing non-Gaussianity, and non-Gaussianity is measured by higher-order moments of distribution such as skewness and kurtosis.

It can be seen from Table 1 that IC1, the factor related to the peripheral countries, has values for kurtosis that exceeds 15.0. Considering the fact that the value of kurtosis is 3.0 for the Gaussian distribution and 12.0 for the Student- $t$  distribution with degrees of freedom 4.5, which is often used in order to describe tail heaviness of return distribution, a kurtosis value exceeding 15 is extremely large, strongly suggesting that the tail risk in the peripheral countries is high. This result suggests the importance of using tail-heavy models for CDS spreads. Such a tail-heavy model includes not only a tail-heavy distribution but also volatility clustering effect which is discussed in Section 4.1.

### **3.3 Selection of financial variables**

Here we consider the financial variables that may be possibly related to the factors impacting the CDS spreads. Longstaff et al. (2011) provide a comprehensive study about the relation between the sovereign CDS spread and financial and economic variables. They investigated the relation between monthly changes of 26 sovereign CDS spreads and 14 financial and economic variables. These variables include local stock market return, change in US corporate yield spread between BBB and AAA credits, change in US

corporate yield spread between BB and BBB credits, change in volatility risk premium (measured as the difference between the implied volatility of the VIX and the realized volatility of S&P 100), and regional and global averages of CDS spreads.<sup>9</sup> These variables are related to the CDS spread. The significance of the other variables in the paper with the CDS spreads varies.

In the context of the systemic risk in the Eurozone, Ang and Longstaff (2013) investigated the relation between seven financial variables and what they refer to as the “intensity of the systemic risk,” computed from their stochastic default intensity model.<sup>10</sup> They computed the intensities for the systemic risk for the US and the Eurozone using the CDS spreads for the US and Germany, respectively. They then investigated which financial variable drives weekly change in the systemic risk intensity. The variables they investigated are market stock returns (S&P500 for the US and DAX for the Eurozone), change in the 5-year constant maturity swap rates (denominated in the US dollar for the US and in the euro for the Eurozone), change in VIX (for both the US and the Eurozone), change in corporate CDS spreads (the CDX North American Investment Grade Index for the US and the European iTraxx Index for the Eurozone), and changes in five foreign CDS spreads (Japan, China, and CDX Emerging Markets). They found that market stock returns, change in corporate CDS spreads, and the CDS spread change for the Chinese government are related to the intensity of systemic risk in both the US and the Eurozone. They also reported that for the US, change in the VIX is related to the systemic risk intensity.

Guided by the variables identified in these two studies, we selected six variables for our

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<sup>9</sup>The other variables are: exchange rates, foreign reserves, US stock market return, change in 5-year US Treasury yields, equity premium, US term premium, and capital flows in bonds and equities.

<sup>10</sup>Ang and Longstaff (2013) proposed a model based on Duffie et al. (2003) that the default intensity of a specific country is the sovereign-specific intensity plus the intensity for the systemic risk (multiplied by a constant specific for the country representing its exposure to the systemic risk). They considered that the default intensity in the CDS spreads for the US Treasuries represents the intensity of the systemic risk for the CDS spreads of US states. Likewise, they regarded the intensity of Germany as the intensity of the systemic risk for the Eurozone sovereign CDS spreads.

analysis. First, since both studies reported that stock returns impact the sovereign CDS spreads, we include two series of stock index returns. The first is the average of logarithmic returns across the three core countries (Belgium, France and Germany). We use the euro-denominated MSCI<sup>11</sup> for the stock index return for each country, and the equally-weighted average for these countries is labeled “stock index of core countries.” The second series is the average of the peripheral countries (Greece, Italy, Portugal and Spain for the seven countries data and Italy, Portugal and Spain for the six countries data). The equally-weighted average for these countries is labeled “stock index of peripheral countries.”

Second, since it was reported that volatility was related to sovereign CDS spreads, we introduced two volatility indices. One is the VSTOXX, an index of volatility implied by the EUROSTOXX 50 options, an index comprised of the most liquid Eurozone stocks representing the risk aversion within the Eurozone. We label this volatility index as the “Eurozone stock implied volatility (VSTOXX).” The other volatility index is the CBOE VIX, an index of volatility implied by the S&P 500 options. Since the US stock market is more global than the Eurozone stock market, we label the VIX “global stock implied volatility (VIX).”

Both Longstaff et al. (2011) and Ang and Longstaff (2013) observed that corporate credit condition is related to the CDS spreads. More specifically, Longstaff et al. (2011) reported that changes in US corporate yield spreads were related to changes in the CDS spreads, and Ang and Longstaff (2013) reported that changes in corporate CDS indexes were related to the systemic risk intensity in CDS spreads both in the US and the Eurozone. As a proxy for credit condition, in this paper we use the Markit iTraxx Europe Index, referring to it as the “Eurozone corporate CDS index.”

Ang and Longstaff (2013) reported that China’s CDS spread was related to the systemic risks of the US and the Eurozone. Longstaff et al. (2011) showed that systemic

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<sup>11</sup>Designed by the Morgan Stanley Capital International before, and by the MSCI Barra today.

risks defined as the first PC of the 26 sovereign CDSs explained more than 60% of their variation. These findings indicate that the Eurozone sovereign CDS market and that of the rest of the world are related, multilaterally affecting each other. In order to represent this relation, we consider four major economies outside of the Eurozone: China, Japan, the United Kingdom, and the Switzerland. We use their equally-weighted average of the CDS spreads denominated in US dollar, labeling it “global sovereign CDS index.”<sup>12</sup>

In addition to these six variables, we consider four variables representing the risk characterizing the Eurozone sovereign debt crisis. The first variable is the one related to the cost for a sovereign state government to maintain the financial system by means such as bail-outs, as reported by Mody (2009). In this paper, we use the Markit iTraxx Europe Senior Financial Index for its continuity and simplicity. We label it “Eurozone financial CDS index.”

The second, third and fourth variables are those representing the risk of redenomination of the Eurozone countries. One of the approaches to measure this risk is to compare the bond yields in different currencies based on the notion that the expected exchange rate change due to redenomination is reflected to the yield difference in different currencies. Krishnamurthy et al. (2013) introduced this idea by using bond yields of Italy, Portugal and Spain denominated in the US dollar and the euro. De Santis (2015) used CDS spreads of France, Italy, Spain and Germany since the USD-denominated bond issued by these countries is scarce. We use the CDS spreads, following De Santis (2015). Accordingly, the redenomination risk  $I$  underlying the CDS spread is defined as follows:

$$I_t^{c,b,h} = (S_t^{c,h,USD} - S_t^{c,h,EUR}) - (S_t^{b,h,USD} - S_t^{b,h,EUR}), \quad (7)$$

where  $S$  denotes a CDS spread, the superscript  $c$  denotes the country referenced by the CDS,  $b$  denotes Germany, USD denotes denomination in US dollar, EUR denotes

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<sup>12</sup>We do not use the US Treasury CDS spread since it is usually denominated in the Euro.

denomination in the euro,  $h$  denotes the maturity, and the subscript  $t$  denotes time.

In order to compute  $I$  in equation (7), we use the US dollar-denominated CDS spreads explained in Section 2, and the euro-denominated 5-year CDS spreads downloaded from the Bloomberg Financial Markets.<sup>13</sup> We consider the redenomination risk  $I$  for Belgium, France, Greece, Portugal and Spain.<sup>14</sup> We compute the equally-weighted average of the values of  $I$  for Belgium and France and label it “redenomination risk of core countries.” We also compute the average of  $I$  for Greece, Portugal, and Spain (for the seven countries data) and for Portugal and Spain (for the six countries data), labeling it “redenomination risk of peripheral countries.”

Finally, the volatility of the exchange rate between the euro and the US dollar would be expected to be related to the redenomination risk because it is related to the valuation of the euro. We use the volatility implied by the three-month at-the-money option of the exchange rate obtained from Bloomberg, labeling it “EURUSD implied volatility.”

Table 4 lists the 10 variables we use in this study.

### 3.4 Link between ICs and financial variables

Here we investigate whether the ICs found in our analysis are related to the financial variables selected in Section 3.3. We estimate a simple regression whose the explanatory variable ( $X$ ) is one of the financial variables we selected, and whose explained variable ( $Y$ ) is one of the PCs or ICs. Since the explained variable (a PC or an IC) has large kurtosis as can be seen from Table 1, it is possible that outlier observations influence the regression result. Therefore, we adopt a robust regression using the Tukey’s biweight

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<sup>13</sup>There are many missing values of the euro-denominated CDS spreads in 2012. We complement these values from the sovereign bond yields, under the assumption that the weekly change of CDS spread is a linear function of that of bond yield. Note that both changes match theoretically since both are denominated in the same currency, the euro.

<sup>14</sup>Germany is excluded since it is used as the basis in equation (7). Italy is excluded for the scarcity of the available data.

Table 4: Definition for the financial variables in this study.

<b>Name</b>	<b>Definition</b>
Stock index of core countries:	Weekly log-return of the EUR-denominated MSCI, equally-weighted average of Belgium, Germany and France. The unit is one percent.
Stock index of peripheral countries:	Weekly log-return of the EUR-denominated MSCI, equally-weighted average of Greece, Italy, Portugal, and Spain. The unit is one percent.
Global stock implied volatility (VIX):	Weekly changes of the CBOE VIX. The unit is one percent.
Eurozone stock implied volatility (VSTOXX):	Weekly changes of the VSTOXX. The unit is one percent.
Eurozone corporate CDS index:	Weekly change of the Markit iTraxx Europe. The unit is one basis point.
Global sovereign CDS index:	Weekly change of 5-year sovereign CDS spreads, equally-weighted average of China, Japan, Switzerland, and the United Kingdom. The unit is one basis point.
Eurozone financial CDS index:	Weekly change of the Markit iTraxx Europe Senior Financials. The unit is one basis point.
Redenomination risk of core countries:	Weekly change of "redenomination risk" defined in equation (7) in section 3.3, equally-weighted average of France and Belgium. The unit is one basis point.
Redenomination risk of peripheral countries:	Weekly change of "redenomination risk" defined in equation (7) in section 3.3, equally-weighted average of Greece, Portugal, and Spain. The unit is one basis point.

Table 5: Simple linear regression results when each PC is set as the explained variable ( $Y$ ) and each financial variable as the explanatory variable ( $X$ ). For estimation of the regression coefficients, robust regression with Tukey’s biweight function is adopted. The single asterisk (\*) means that the regression coefficient deviates from zero using a significance level of 5%, and the double asterisk (\*\*) means that the regression coefficient deviates from zero using a significance level of 1%. The  $R^2$  values are those obtained from applying ordinary least squares.

X=	Y=PC1		Y=PC2		Y=PC3	
	coeff.	R2	coeff.	R2	coeff.	R2
Seven countries from January 2009 to June 2011						
Stock index of core countries	-0.42 **	0.30	-0.03	0.00	-0.01	0.01
Stock index of peripheral countries	-0.46 **	0.49	-0.02	0.00	0.00	0.01
Global stock implied volatility (VIX)	0.21 **	0.13	0.02	0.03	0.01	0.02
Eurozone stock implied volatility (VSTOXX)	0.24 **	0.15	0.02	0.02	0.01	0.02
Eurozone corporate CDS index	0.18 **	0.48	0.02 **	0.00	0.00	0.00
Global sovereign CDS index	0.29 **	0.43	0.04 **	0.04	0.00	0.00
Eurozone financial CDS index	0.13 **	0.53	0.01 *	0.01	-0.01 *	0.00
Redenomination risk of core countries	0.20 **	0.06	-0.01	0.00	-0.03 *	0.03
Redenomination risk of peripheral countries	0.05 **	0.07	0.00	0.02	0.00	0.00
EURUSD implied volatility	1.25 **	0.18	0.03	0.04	-0.08	0.00
Six countries from January 2009 to December 2013						
Stock index of core countries	-0.41 **	0.32	-0.04 **	0.00	0.02 *	0.00
Stock index of peripheral countries	-0.41 **	0.42	-0.02	0.00	0.02 *	0.00
Global stock implied volatility (VIX)	0.28 **	0.17	0.03 **	0.01	0.00	0.00
Eurozone stock implied volatility (VSTOXX)	0.26 **	0.17	0.03 **	0.00	-0.01	0.00
Eurozone corporate CDS index	0.15 **	0.45	0.01 *	0.00	0.00	0.00
Global sovereign CDS index	0.25 **	0.34	0.04 **	0.03	0.00	0.00
Eurozone financial CDS index	0.09 **	0.49	0.00	0.00	-0.01 **	0.01
Redenomination risk of core countries	0.07 **	0.04	-0.01	0.01	-0.01 *	0.02
Redenomination risk of peripheral countries	0.01	0.01	0.00 *	0.03	0.00	0.00
EURUSD implied volatility	1.33 **	0.21	0.02	0.01	-0.03	0.00

function.<sup>15</sup> Tables 5 and 6 show the results of the simple regressions for the PCs and the ICs, respectively. It shows regression coefficients, the significance of these coefficients (‘\*’ and ‘\*\*’ denote the levels of 1% and 5%, respectively), and  $R^2$  values.<sup>16</sup>

For PC results reported in Table 5, all financial variables except the redenomination risk of peripheral countries are found to be significantly related to PC1. The signs of the regression coefficients are negative for the stock index returns and are positive for the

<sup>15</sup>The weight for an outlier residual  $\varepsilon = sr$  is given as  $[\max\{0, 1 - r^2/k^2\}]^2$  where  $s$  is the estimated standard deviation of residuals. Here we adopt  $k = 4.685$ .

<sup>16</sup>The  $R^2$  values here are those based on the ordinary least squares.

Table 6: Simple linear regression results when each IC is set as the explained variable ( $Y$ ) and each financial variable as the explanatory variable ( $X$ ). For estimation of the regression coefficients, robust regression with Tukey's biweight function is adopted. The single asterisk (\*) means that the regression coefficient deviates from zero using a significance level of 5%, and the double asterisk (\*\*) means that the regression coefficient deviates from zero using a significance level of 1%. The  $R^2$  values are those obtained from applying ordinary least squares.

X=	Y=IC1		Y=IC2		Y=IC3	
	coeff.	R2	coeff.	R2	coeff.	R2
Seven countries from January 2009 to June 2011						
Stock index of core countries	-0.04	0.11	-0.11 **	0.11	-0.11 **	0.09
Stock index of peripheral countries	-0.07 **	0.17	-0.10 **	0.17	-0.12 **	0.16
Global stock implied volatility (VIX)	0.02	0.13	0.06 **	0.03	0.04	0.01
Eurozone stock implied volatility (VSTOXX)	0.02	0.13	0.07 **	0.05	0.05 *	0.01
Eurozone corporate CDS index	0.01	0.17	0.03 **	0.15	0.05 **	0.16
Global sovereign CDS index	0.02	0.05	0.08 **	0.24	0.10 **	0.26
Eurozone financial CDS index	0.01 *	0.22	0.01 **	0.10	0.05 **	0.22
Redenomination risk of core countries	0.02	0.00	-0.01	0.00	0.08 **	0.09
Redenomination risk of peripheral countries	0.01 **	0.07	0.01	0.01	0.01	0.02
EURUSD implied volatility	0.02	0.15	0.09	0.01	0.26 *	0.05
Six countries from January 2009 to December 2013						
Stock index of core countries	-0.04 **	0.05	-0.08 **	0.08	-0.18 **	0.20
Stock index of peripheral countries	-0.05 **	0.12	-0.06 **	0.07	-0.16 **	0.25
Global stock implied volatility (VIX)	0.03 **	0.09	0.05 **	0.03	0.10 **	0.06
Eurozone stock implied volatility (VSTOXX)	0.02	0.05	0.06 **	0.05	0.10 **	0.08
Eurozone corporate CDS index	0.02 **	0.12	0.03 **	0.10	0.05 **	0.24
Global sovereign CDS index	0.03 **	0.05	0.08 **	0.21	0.08 **	0.15
Eurozone financial CDS index	0.01 **	0.12	0.01 **	0.06	0.04 **	0.31
Redenomination risk of core countries	0.02 *	0.01	-0.01	0.00	0.03 **	0.06
Redenomination risk of peripheral countries	0.01 **	0.03	0.00	0.01	0.00	0.00
EURUSD implied volatility	0.16 **	0.12	0.17 **	0.03	0.37 **	0.07

other variables, which is an intuitive result. As for  $R^2$ , the values for the stock index of peripheral countries and for the Eurozone financial and corporate CDS indexes range from 0.42 to 0.53. These results show that PC1 is an important component.

In contrast, the regression results for PC2 and PC3 are less informative. PC2 is significantly related to several financial variables. However, the  $R^2$  values are less than 0.05 for all the cases, showing that these variables cannot explain the variation of PC2. As for PC3, the regression coefficient is not significant for most cases, and their signs are difficult to interpret.

Table 6 shows the result for the ICs. Observing the results for each IC, we see that all ICs have more than one financial variable that is significantly related to with large  $R^2$  values. For example, for both datasets IC1 can be related to the stock index of peripheral countries, the Eurozone financial CDS index, and the redenomination risk of peripheral countries. IC2 can be related to the stock indices (of the core and the peripheral countries), the stock implied volatilities (of the global and the Eurozone), and the CDS indices (of the Eurozone corporate, the global sovereign, and the Eurozone financial). IC3 can be related to the stock indices, the Eurozone stock implied volatility (VSTOXX), the CDS indices, the redenomination risk of core countries, and the EURUSD implied volatility.

In turn, the results for each financial variable indicates that some of the financial variables have a selective effect on ICs. The stock index of core countries is significant for IC2 and IC3 but not for IC1 in both datasets. The global stock implied volatility (VIX) is significant only for IC2. The Eurozone stock implied volatility (VSTOXX) and the CDS indices (Eurozone corporate CDS index, Global sovereign CDS index, and Eurozone financial CDS index) are significant for both IC2 and IC3. The redenomination risk of core countries is significant for IC3, while the redenomination risk of peripheral countries is significant for IC1. The EURUSD implied volatility is significant only for

IC3.

These results support the interpretation of ICs that we proposed in Section 3.2. There we reported that IC1 can be interpreted as the factor related to the risk of the peripheral countries. The regression results above support this idea, since IC1 is related to peripheral variables such as the stock index return of peripheral countries and the redenomination risk of peripheral countries. IC3 is exclusively related to the redenomination risk of core countries and the EURUSD implied volatility, in addition to the stock returns and the CDS indices. This supports the view that IC3 represents the risk common to the Eurozone.

In Section 3.2 we observed that IC2 can be considered to be a factor of core countries. However, the above results indicate that IC2 is exclusively related to the global stock implied volatility (VIX), and also is related to the global sovereign CDS spreads. Since the markets of core countries such as Germany and France are connected to global financial markets in the same way that the US market is, it is not surprising that the factor representing core countries is related to global financial market variables. Therefore, we can interpret IC2 as the global risk factor.

In summary, based on the factor loadings and the regression by financial variables, we can interpret the three ICs as the peripheral risk factor, the global risk factor, and the Eurozone common risk factor. Figure 2 provides a comparison between the cumulative sum of each IC and the level of one of the variables significantly related to the IC. We selected the stock index of peripheral countries for the cumulative sum of  $IC1 \times (-1)$ ,<sup>17</sup> the global sovereign CDS index for IC2, and the Eurozone financial CDS index for IC3. From the figure the relations between the ICs and the financial variables are observed.

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<sup>17</sup>We multiplied  $(-1)$  in order that the stock returns and IC1 change in the same direction.

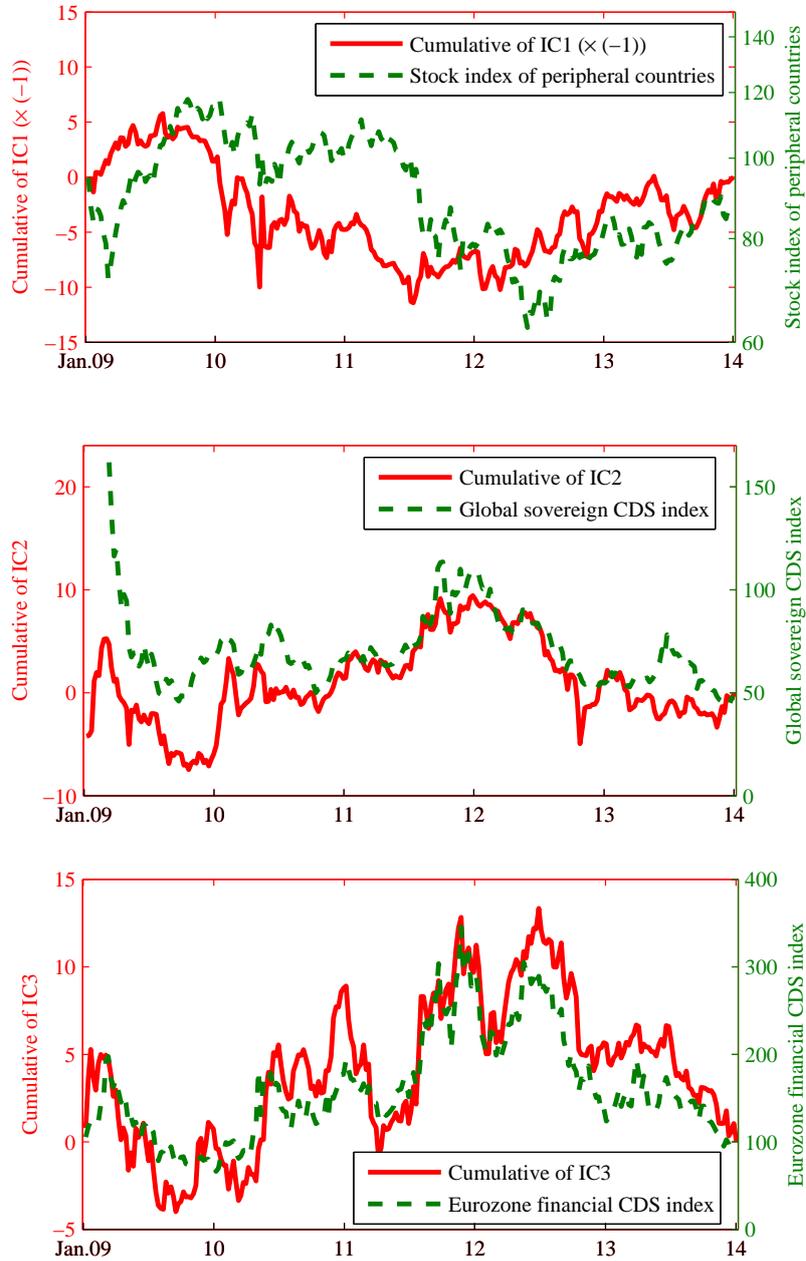


Figure 2: Comparison between the cumulative sum of each IC and the levels of variables in relation with the IC. Note that the cumulative sum of IC1 is inverted since the regression coefficients between IC1 and the stock index of peripheral countries is negative.

## 4 Analyses based on the ICA model

In this section, we propose possible analyses based on the ICA model given by equation (4). We first introduce the conditional volatility of the ICs, and consider the dynamic correlation based on that, showing the decoupling of the Eurozone sovereign CDS markets. We also show the PDF of the ICA-based models and propose an example of model comparison based on the likelihood.

Hereafter, we assume that the components of  $\mathbf{s}$  are independent and therefore each component of  $\mathbf{s}$  can be modeled by a one-dimensional distribution. This is a major advantage compared to the other multivariate models because it reduces a good deal of computational burden tied to multivariate models.

### 4.1 Volatility of the ICs

Because the changes of the CDS spreads in the crisis period are volatile, the log-returns of CDS are expected to have a volatility clustering effect, and so are the ICs. In fact, by using the statistical test proposed by Engle (1982), IC1 and IC2 are expected to exhibit a volatility clustering effect.<sup>18</sup> Therefore we apply GARCH(1,1) model<sup>19</sup> to  $s_{jt}$ :

$$\left\{ \begin{array}{l} s_{jt} = \sigma_{jt}^{(s)} \varepsilon_{jt}, \\ (\sigma_{j,t+1}^{(s)})^2 = \omega_j + a_j s_{jt}^2 + b_j \sigma_{jt}^2, \\ E \varepsilon_{jt} = 0, \text{var} \varepsilon_{jt} = 1. \end{array} \right. \quad (8)$$

Figure 3 shows the volatility of the ICs obtained from the GARCH(1,1) model with the standardized Student- $t$  distribution.<sup>20</sup> The historical (26 weeks backward) volatility

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<sup>18</sup>The null hypothesis of no serial correlation in the squared ICs is rejected for IC1 up to at least 8 lags for both datasets with 99% significance level. For IC2, the null is rejected for most lags up to 10 with 90% significance level, many of which can be rejected with 99% significance. However, the null for IC3 cannot be rejected for most cases.

<sup>19</sup>This specification is popular; see Hansen and Lunde (2005).

<sup>20</sup>Here the Student- $t$  distribution is multiplied by  $\sqrt{\nu - 2/\nu}$  in order to set the variance to unity, where

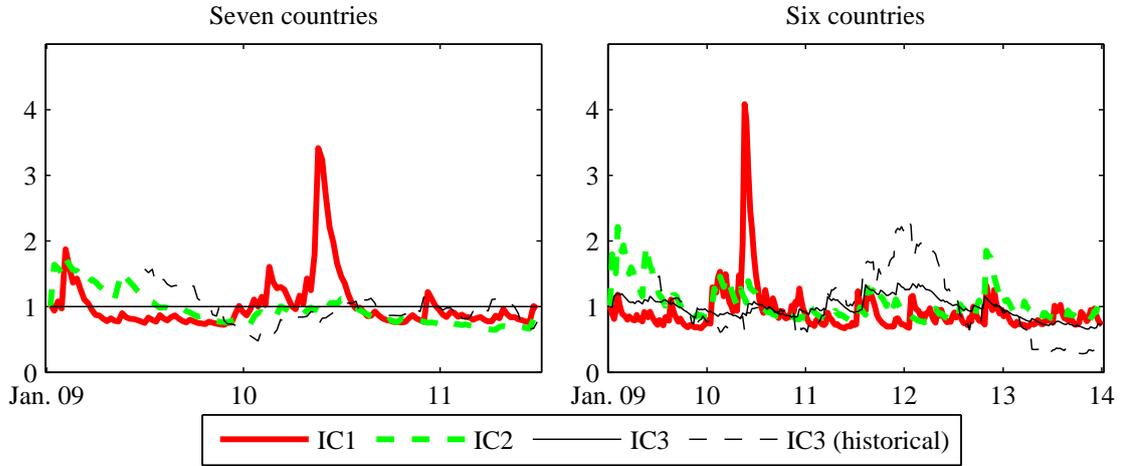


Figure 3: Volatilities of the ICs obtained. All series except “IC3 (historical)” are obtained by the GARCH(1,1) model with standardized Student- $t$  residuals. The series labeled “IC3 (historical)” shows the historical volatility of IC3 with the length of window 26.

is also shown for IC3 since using the ARCH model in this case cannot be statistically justified.

From the figure, the volatility of IC1, the peripheral factor, spiked to a level more than 4.0 in May 2010. Before this spike, the volatility of IC1 started increasing around the beginning of 2010, showing the increasing concern for the peripheral countries. The spike in May 2010 shows the magnitude of the concern for the events in Greece at that time (see Section 2), which invoked the following crisis that the Eurosystem confronted. After May 2010, the volatility of IC1 had calmed down as indicated by a decline in its level to around 1.0, showing that the concern shifted from the risk in periphery to the other source of risk.

The volatility of IC2, the global factor, was high at the beginning of 2009. This is related to the remaining effect from the US financial crisis in 2008, which is considered to have a global effect. The volatility of IC2 during the Eurozone sovereign debt crisis post-2010 was relatively stable compared to IC1.

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$\nu$  is the number of degrees of freedom.

As for IC3 in the six country data, its GARCH volatility widened towards the beginning of 2012.<sup>21</sup> This widening becomes clearer by looking at its historical volatility. In contrast, the volatilities of IC1 and IC2 remained low around that time. So IC3, the Eurozone common factor, can be considered as the major source of volatility during the period around 2012. As we discussed in Section 1, the risk specific to this period was the risk of redenomination in the Eurozone. The result shows the possibility that the redenomination risk comes from the common factor to the Eurozone, not from the reasons specific to peripheral countries.

These different peaks for the volatilities indicates the shift of the volatility source of the Eurozone sovereign CDS spreads. That is, the volatility source was the global factor in 2009, but then shifted to the peripheral factor in 2010, and to the Eurozone common factor in 2011 to 2012. These different risk sources would correspond to different stages of the Eurozone sovereign debt crisis.

Note that the sharp increase for IC1 volatility can be observed in the six countries data which do not contain the information about Greece. This suggests that ICA can reconstruct the risk of the peripheral countries including Greece from the information excluding Greece.

## 4.2 Dynamic correlation

Based on equation (8), the dynamic variance and covariance of returns can be derived. To do so, we follow Kumiega et al. (2011) and García-Ferrer et al. (2012). We assume

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<sup>21</sup>The GARCH volatility of IC3 for the seven countries data seems almost flat. This is because its historical volatility is close to flat, suggesting that the GARCH model may not be suitable in this case.

that the volatility of  $\mathbf{s}_t$  is time dependent and that of  $\mathbf{p}^b_t$  in (6) is constant:

$$\text{var}_t(s_{jt}) = (\sigma_{jt}^{(s)})^2, \quad j = 1, \dots, q, \quad (9)$$

$$\text{var}_t(p_{jt}) = (\sigma_j^{(p)})^2, \quad j = q + 1, \dots, d, \quad (10)$$

where  $\text{var}_t$  mean that the variance measured at time  $t$ . From equations (4) and (6) we obtain

$$\begin{aligned} \text{cov}_t(\mathbf{r}_t) &= A \times \text{cov}_t(\mathbf{s}_t) \times A^\top + \text{cov}_t \varepsilon_t \\ &= A \times \text{diag}[(\sigma_{1t}^{(s)})^2, \dots, (\sigma_{qt}^{(s)})^2] \times A^\top \\ &\quad + D_r^{1/2} U_b \text{diag}[(\sigma_{q+1}^{(p)})^2, \dots, (\sigma_d^{(p)})^2] U_b^\top D_r^{1/2}. \end{aligned} \quad (11)$$

The dynamic correlation between  $r_{tj_1}$  and  $r_{tj_2}$  is then defined as

$$\rho_{t,j_1,j_2} = \frac{\text{cov}_t(r_{t,j_1}, r_{t,j_2})}{\sqrt{\text{var}_t(r_{t,j_1})\text{var}_t(r_{t,j_2})}}. \quad (12)$$

Figure 4 shows the pairwise dynamic correlations for the seven countries. The red bold line labeled “ICA” shows the dynamic correlation based on equation (12). The black dashed line labeled “rolling” shows the historical correlation during the rolling-window period consisting of 26 weeks prior to the designated date. In addition to these correlations, for the purpose of comparison, we also show the dynamic correlation based on the conditional Gaussian copula model proposed by Patton (2006), which is shown by the blue thin sold line labeled “Conditional copula”.

From Figure 4 it can be observed that the ICA correlations between the peripheral countries and Germany (DE-IT, DE-ES, DE-PT, DE-GR) decreased toward the middle of 2010. The ICA correlation between the peripheral countries (IT-GR, ES-GR, PT-GR, and IT-PT, for example) increased toward the middle of 2010. These correlations strongly

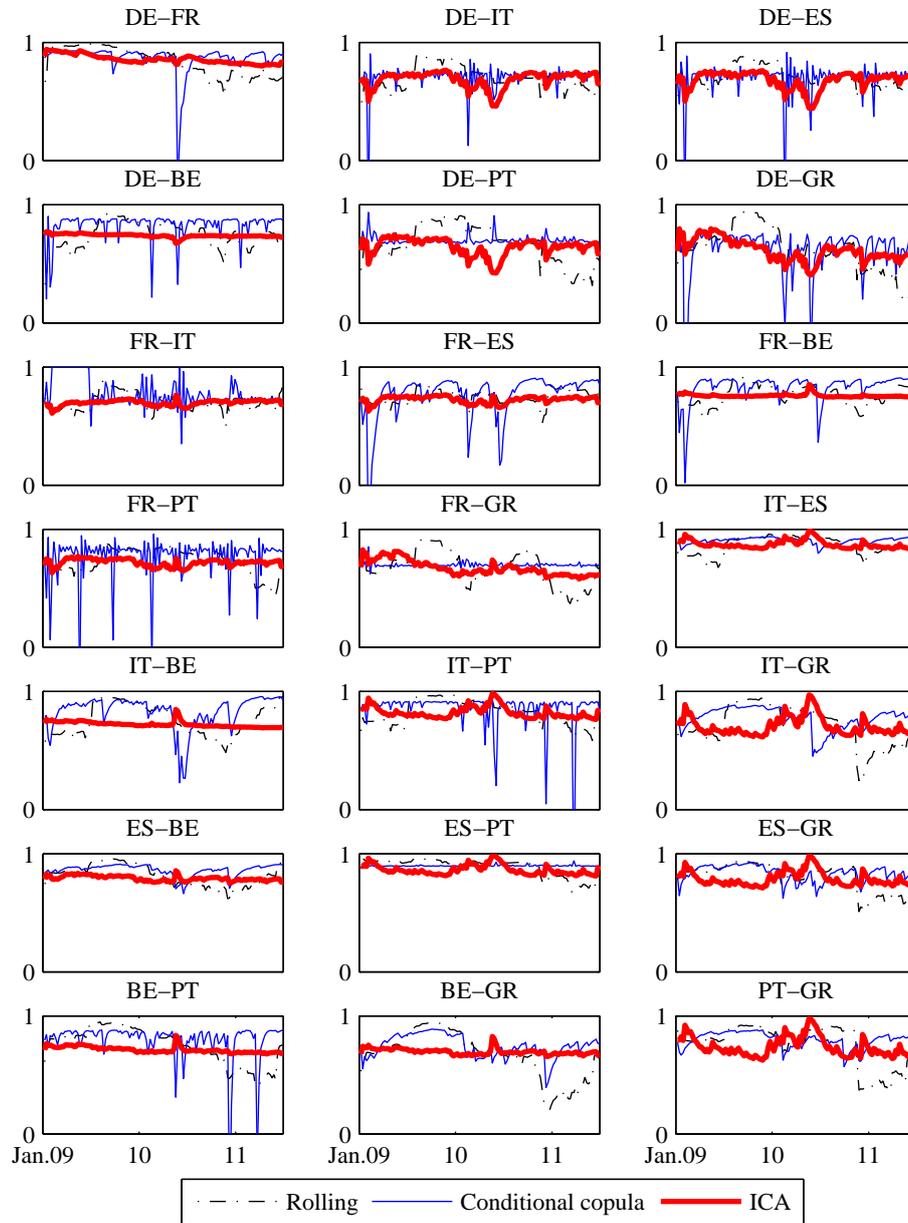


Figure 4: Dynamic correlations between the seven countries. The dynamic correlations are obtained by the three different methods: the historical correlation during the rolling-window (black dashed lines labeled “Rolling”), the correlation based on conditional copula model (blue thin lines labeled “Conditional copula”), and the correlation based on the ICA model combined with the GARCH model (red bold lines labeled “ICA”).

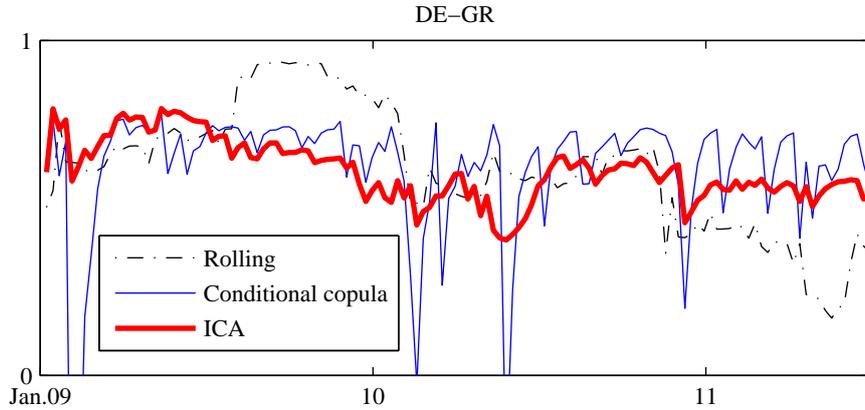


Figure 5: Dynamic correlations between Germany and Greece (based on the seven countries data). The dynamic correlations are obtained by the three different methods: the historical correlation during the rolling-window (black dashed line labeled as “Rolling”), the correlation based on conditional copula model (blue thin line labeled “Conditional copula”), and the correlation based on the ICA model combined with the GARCH model (red bold line labeled “ICA”).

suggest the increasing disparity between the Eurozone sovereign CDS spreads during the period investigated.

Figure 5 enlarges the chart of the dynamic correlation between Germany and Greece from Figure 4. From the figure, the rolling correlation between Germany and Greece is close to unity in 2009, while it slides down to around 0.5 since 2010 as the Greek crisis deepened. In the ICA correlation, the correlation stays in the range 0.6 to 0.8 in 2009, and since 2010 descends gradually to the range 0.4 to 0.6 since 2010. In May 2010, the ICA correlation drops down to 0.4, which is not evident in the rolling correlation. As we indicated in Section 2, at that time the hidden debt of the Greek government was revealed and, as a result, the solvency of the country came into question. The decline in ICA correlation can be considered to be the market’s immediate response, which is not evident by simply looking at the rolling correlation.

From Figure 5, the correlation based on the dynamic Gaussian copula model also drops sharply in May 2010, indicating that both models can detect the sharp decrease in the

correlation. It seems that in 2010, the dynamic Gaussian copula exhibits more sensitive movements compared to the ICA correlation, that is, the ICA correlation decreases slowly before the dynamic Gaussian copula model shows immediate and sharp decreases. From these observations, it is fair to say that the ICA correlation provides a dynamic correlation whose feature is different from that provided by the dynamic copula model. An advantage of the ICA correlation compared to the rolling correlation or the dynamic copula model is that we can distinguish the factor of high volatility and high risk, as explained in Section 4.1.

### 4.3 ICA model likelihood

In this paper, we compare model fitness by using likelihood function. We derive a simple formula for the likelihood of models based on equations (4) and (8). Let  $f_X(\cdot)$  denote the PDF of a random scalar or vector  $X$ , hereafter.

#### 4.3.1 The case $q = d$

For simplicity, we first consider the case  $q = d$ , that is, the number of components  $q$  is equal to the number of the data dimension  $d$ . In this case the noise term  $\epsilon_t$  in equations (4) satisfies  $\epsilon_t \equiv 0$ , and we obtain  $\mathbf{r}_t = \mu + A\mathbf{s}_t$ .

Using the formula for the change of variables (Jacobian transformation) and the factorization of  $f_{\mathbf{s}_t}$  in equation (2), we obtain

$$\begin{aligned} f_{\mathbf{r}_t}(\mathbf{r}_t) &= \frac{1}{|\det A|} f_{\mathbf{s}_t}(\mathbf{s}_t) \\ &= \frac{1}{|\det A|} f_{s_{1t}}(s_{1t}) \cdots f_{s_{dt}}(s_{dt}), \end{aligned} \tag{13}$$

For the unconditional  $S_j$ , the distribution of  $\mathbf{r}_t$  is

$$f(\mathbf{r}_1, \dots, \mathbf{r}_T) = \frac{1}{|\det A|^T} \prod_{j=1}^d \prod_{t=1}^T f_{S_j}(s_{jt}). \quad (14)$$

For the GARCH-type conditional distribution in equation (8),  $f_{s_{j1}, s_{j2}, \dots, s_{jT}}$  is factorized as

$$\begin{aligned} f_j(s_{j1}, s_{j2}, \dots, s_{jT}) &= f_{j1}(s_{j1})f_{j2|1}(s_{j2}) \cdots f_{jT|T-1}(s_{jT}), \\ &= \frac{f_\varepsilon(\varepsilon_{j1})}{\sigma_{j1}} \cdot \frac{f_\varepsilon(\varepsilon_{j2})}{\sigma_{j2}} \cdots \frac{f_\varepsilon(\varepsilon_{jT})}{\sigma_{jT}} \end{aligned} \quad (15)$$

where  $f_{jt|t-1}(s_{jt})$  is the PDF of  $s_{jt}$  conditional to the information up to time  $t - 1$  and  $f_\varepsilon = f_\varepsilon(\varepsilon)$  is the PDF of the residuals  $\varepsilon$  independent of  $t$ . Therefore, we can derive the PDF as

$$f(\mathbf{r}_1, \dots, \mathbf{r}_T) = \frac{1}{|\det A|^T} \prod_{j=1}^d \prod_{t=1}^T \frac{f_\varepsilon(\varepsilon_{jt})}{\sigma_{jt}}. \quad (16)$$

Equations (14) and (16) are the formula for computing the likelihood of an ICA-based model. Together with these equations, we compute the likelihood of the data, allowing us to compare the model with other models that we review in Section 4.4.

### 4.3.2 The case $q < d$

Next we consider the general case  $q < d$ . In order to derive a simple formula for the PDF, we adopt two reasonable assumptions based on the interpretation that  $\epsilon_t$  represents noise. The first assumption is that factors  $\mathbf{s}_t$  and noises  $\epsilon_t$  are independent of each other. Second, according to equation (6),  $\epsilon_t$  is a linear combination of  $(d - q)$  PCs  $\mathbf{p}^{\mathbf{b}}_t = (p_{q+1,t}, \dots, p_{dt})^\top$ . Interpreting these  $(d - q)$  PCs as independent noise sources, we assume that they are independent of each other. Accepting these assumptions, we obtain the following formula

for the PDF of equation (4):

$$f_{\mathbf{r}_t}(\mathbf{r}_t) = \frac{1}{|\det D_r^{1/2} \det A_{\text{IC}}|} \prod_{j=1}^q f_{S_{jt}}(s_{jt}) \prod_{j=q+1}^d f_{p_{jt}}(p_{jt}), \quad (17)$$

where  $A_{\text{IC}}$  is a  $q$ -by- $q$  matrix defined as  $A = D_r^{1/2} U_a A_{\text{IC}}$  and  $U_a$  is the left  $q$  columns of  $U$  in equation (3).

#### 4.4 Model comparison based on likelihood

Next we consider the goodness-of-fit of the ICA-based model, equation (4), using the likelihood function obtained in Section 4.3. In Section 3.1 we consider the ICA model of  $q = 3$ , and in Section 4.1 we consider the GARCH(1,1) model in equation (8). We refer to the GARCH(1,1) model for the case  $q = 3$  as the *ICA-GARCH- $T$  dimension reduction* model. In this model we use the Student- $t$  distribution with a scale parameter as the distribution of the noise  $p_{jt}$ .

For purposes of comparison, we apply five additional models to the CDS spreads. The first model is the *multivariate Gaussian* model:

$$\mathbf{r}_t \sim N(\boldsymbol{\mu}, \boldsymbol{\Sigma}), \quad (18)$$

where  $\boldsymbol{\mu}$  is a vector representing mean and  $\boldsymbol{\Sigma}$  is a matrix representing covariance.

The second model is the GARCH(1,1) model with Gaussian marginal and copula (the idea of copula is explained below). The model is specified by equations (8) and

$$\left\{ \begin{array}{l} r_{jt} = \mu_j + s_{jt}, \\ \varepsilon_{jt} = \Phi^{-1}(u_{jt}), \\ \mathbf{U}_t = (u_{1t}, \dots, u_{dt})^\top \sim C_G(\boldsymbol{\Sigma}), \end{array} \right. \quad (19)$$

where  $\Phi^{-1}$  is the inverse cumulative distribution function of the standard Gaussian distribution and  $C_G(\Sigma)$  denotes the Gaussian copula with correlation parameter matrix  $\Sigma$ . This is a popular model to incorporate volatility clustering effect to multivariate series. We label the model the *GARCH-Gaussian marginal and copula* model.

The third and the fourth models are the ICA-based models. In the third model, we obtain the ICs without dimension reduction. So we obtain  $d$  series of the ICs, and we apply GARCH(1,1) with Student- $t$  residuals to each IC. We consider the possibility of loss of information due to dimension reduction by this model. We label this model the *ICA-GARCH- $T$  no dimension reduction* model. In the fourth model, we obtain  $d$  ICs with no dimension reduction, and apply the standardized Student- $t$  distribution for each ICs. Using this model, we consider the difference between homoscedastic and heteroscedastic models for the ICs. We label this model the *ICA- $T$  no dimension reduction* model.

The fifth model is based on the theory of *copula* distribution, which is a popular statistical concept to describe the dependency structure of multiple variables. A copula function has the advantage that it can describe the nonlinear structure of dependence that would be impossible to express by linear models such as ICA, PCA or FA (Joe, 1997; Nelsen, 2007). A Gaussian copula is popular since it is easy to implement. In this model we use a Student- $t$  copula as a dependency structure, which can describe important dependence structures between variables such as tail dependence (Demarta and McNeil, 2005). Because marginal distributions must be specified when using a copula, we use Student- $t$  distributions for the marginals. We refer to the following model as the *Student- $t$  marginal and copula* model:

$$\begin{cases} r_{jt} = \mu_j + \sigma_j F_{\text{tstd}(\nu_j)}^{-1}(u_j), \\ \mathbf{U} = (u_1, \dots, u_d)^\top \sim C_t(\Sigma, \nu), \end{cases}$$

where  $F_{\text{tstd}(\nu_j)}^{-1}(u_j)$ ,  $j = 1, \dots, d$ , is the inverse cumulative density function of the standard-

Table 7: Log likelihood and Akaike information criteria. The first column gives the name of each model. The second column shows the number of parameters in the model. The parenthesized numbers are the ranks of the models among the five models studied. Commas denote thousand separators.

Models and numbers of parameters		Log likelihood		AIC		BIC	
Seven countries from January 2009 to June 2011							
ICA-GARCH-T dimension reduction	51	1,216	(4)	-2,329	(4)	-2,183	(4)
Multivariate Gaussian	35	1,134	(6)	-2,199	(6)	-2,098	(6)
GARCH-Gaussian marginal and copula	42	1,171	(5)	-2,258	(5)	-2,138	(5)
ICA-GARCH no dimension reduction	63	1,266	(1)	-2,407	(1)	-2,226	(3)
ICA-T no dimension reduction	42	1,245	(2)	-2,406	(2)	-2,286	(1)
Student-t marginal and copula	43	1,234	(3)	-2,383	(3)	-2,259	(2)
Six countries from January 2009 to December 2013							
ICA-GARCH-T dimension reduction	42	2,223	(4)	-4,362	(4)	-4,212	(4)
Multivariate Gaussian	27	2,087	(6)	-4,120	(6)	-4,024	(6)
GARCH-Gaussian marginal and copula	33	2,186	(5)	-4,306	(5)	-4,188	(5)
ICA-GARCH no dimension reduction	51	2,286	(1)	-4,470	(1)	-4,288	(2)
ICA-T no dimension reduction	33	2,227	(3)	-4,389	(3)	-4,271	(3)
Student-t marginal and copula	34	2,242	(2)	-4,417	(2)	-4,295	(1)

ized Student- $t$  distribution with the degree of freedom  $\nu_j$ , and  $C_t(\Sigma, \nu)$  is the Student- $t$  copula distribution with the correlation matrix parameter  $\Sigma$  and the degree of freedom  $\nu$ .

We consider the likelihood of these models. In addition, to penalize the number of parameters, we use the Akaike and the Bayesian information criteria (the AIC and the BIC). Table 7 shows the result for the values of the log-likelihood, the AIC, and the BIC. The number in parentheses is the rank among the six models.

The ICA-GARCH-T dimension reduction model exhibits a better fitting than the multivariate Gaussian or the GARCH-Gaussian marginal and copula models, demonstrating the advantage of the ICA model in comparison to the Gaussian model. In contrast, the ICA-GARCH-T dimension reduction model is always worse than the ICA-GARCH-T no dimension reduction model, the ICA-T no dimension reduction model, and the Student- $t$  marginal and copula models. Therefore, it can be seen that dimension reduction reduces the goodness-of-fit, indicating that dimension reduction results in a lot of information

loss.

Among these no-dimension-reduction models, the ICA-GARCH-T no dimension reduction model is shown to provide a better fit than the Student- $t$  marginal and copula model based on the log-likelihood and the AIC. Also, the ICA-T no dimension reduction model is shown to provide a better fit than the Student- $t$  marginal and copula model for some cases. Considering that the copula-based model can incorporate nonlinear dependence between variables, it is surprising that either the ICA-GARCH-T or the ICA-T models, which are linear models, show better fits than the copula model.

The comparison between the ICA-GARCH-T no dimension reduction and the ICA-T no dimension reduction models shows that the model's fit is improved by considering the volatility clustering effect of the ICs.

Based on these observations, it is fair to conclude that the ICA model provides a good fit to the CDS spread data. Dimension reduction reduces the goodness-of-fit, but the reduced model is still better than popular models such as the GARCH model, and comparable to the complicated dependence model such as Student- $t$  copula model. As for volatility clustering, it is better to incorporate the effect into the model.

## 5 Conclusion

In this paper, we investigated the behavior of Eurozone sovereign CDS spreads during the period of the Eurozone sovereign debt crisis. For that purpose, we introduced a novel technique of factor decomposition, independent component analysis (ICA). We first showed that ICA can find multiple factors impacting CDS spreads, while principal component analysis (PCA) finds one factor. We identified three factors based on ICA, and we found interpretations for these three factors by combining the factor loadings and the regression analysis with financial variables. The first IC was interpreted as the factor

related to the risk associated with the peripheral countries such as Greece and Portugal. The second IC was interpreted as the factor related to global risk. The third IC was interpreted as the factor related to the risk common to the Eurozone. More specifically, we showed that there were two risks specific to the Eurozone sovereign CDS spreads, that is, the risk of the financial sector and the risk of redenomination, are related to these three factors.

Next, we considered several analyses based on ICA. By applying GARCH, we found that the three factors identified had different peaks during the crisis. These different peaks indicated that the source of risk was the global factor in 2009, but it shifted to the peripheral factor in 2010, and finally shifted to the Eurozone common factor in 2012. Utilizing this GARCH volatility, we found that the dynamic correlation based on the ICA model can explain the decoupling between the core and peripheral countries, such as between Germany and Greece. Finally, we compared the ICA model to alternative models by using the likelihood, the AIC and the BIC, showing that the goodness-of-fit of the ICA model is generally better than the other models such as the GARCH and Gaussian marginal and copula model and the Student- $t$  marginal and copula model.

The contributions of the findings of this paper are threefold. Our principal contribution is the finding that there were multiple factors impacting the Eurozone sovereign CDS spreads. This multiplicity is important for explaining the CDS spreads during the Eurozone crisis since it can reasonably explain the reported decoupling of the Eurozone sovereign countries. Second we provided a reasonable interpretation of these factors based on our statistical analysis (regression analysis with financial variables, volatility analysis, and dynamic correlation analysis). Third, our empirical analysis demonstrated why ICA is a more effective statistical tool to employ compared to the more commonly used tool, PCA.

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