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**Purchasing Power Parity for Traded and Non-traded Goods:  
A Structural Error Correction Model Approach**

Jaebeom Kim\* and Masao Ogaki\*\*

**Abstract**

When univariate methods are applied to real exchange rates, point estimates of autoregressive coefficients typically imply very slow rates of mean reversion. However, a recent study by Murray and Papell (2002) calculates confidence intervals for estimates of half-lives for long-horizon and post-1973 data, and concludes that univariate methods provide virtually no information regarding the size of the half-lives. This paper estimates half-lives with a system method based on a structural error correction model for the nominal exchange rate, a domestic price index, a foreign price index, and a monetary variable. The method is applied to estimate half-lives of real exchange rates based on producer price indices, consumer price indices, and GDP implicit deflators. The idea is that the traded good component of the producer price index is proportionately larger than that of the consumer price index. If the convergence rate is faster for traded good prices than that for non-traded good prices, half-lives for the real exchange rate based on the producer price index should be shorter than those for the real exchange rate based on the consumer price index and that on the GDP implicit deflator. Our empirical results are consistent with this view.

**Key words:** Structural Error Correction Model (SECM); Purchasing Power Parity; Real Exchange Rate; Half-life, Convergence Rate

**JEL classification:** C22, F31, F41

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## 1. Introduction

When univariate methods are applied to real exchange rates, point estimates of autoregressive coefficients typically imply very slow rates of mean reversion. Rogoff (1996) discusses that the remarkable consensus of 3-5 year half-lives of purchasing power parity (PPP) deviations is found among studies using long-horizon data. However, a recent study by Murray and Papell (2002) calculates confidence intervals for estimates of half-lives for long-horizon and post-1973 data, and concludes that univariate methods provide virtually no information regarding the size of the half-lives. This paper estimates half-lives of real exchange rates based on producer price indices (PPI), consumer price indices (CPI), and GDP implicit deflators with a system method developed by Kim (2003), who modified Kim, Ogaki, and Yang's estimation method for a Structural Error Correction Model (ECM). This system method employs a two-good version of Mussa's (1982) model with a modification in which the exchange rate exhibits overshooting as in Dornbush's (1976) model. The model includes a gradual adjustment equation, in which the domestic price of the traded good adjusts to the long-run equilibrium level determined by PPP.

In a class of structural ECMs, a single equation instrumental variable (IV) method can be applied to the gradual adjustment equation which describes a gradual adjustment of economic variables toward long-run equilibrium in order to consistently estimate the structural speed of adjustment coefficient. Kim, Ogaki, and Yang's (2003) system method combines the single equation IV method with Hansen and Sargent's (1982) method, which applies Hansen's (1982) Generalized Method of Moments (GMM) to linear rational expectations models.

In the context of Mussa's (1982) model, the gradual adjustment equation implies the first order autoregression for the real exchange rate defined by the domestic and foreign traded good prices. The autoregressive coefficient is one minus the structural speed of adjustment coefficient in the structural ECM. Thus the structural speed of adjustment coefficient can be simply estimated by applying ordinary least squares (OLS) to the real exchange rate autoregression. This coefficient can also be estimated by applying Hansen and Sargent's method to a system of variables containing the nominal exchange rate, the foreign traded good price, and money supply. The system method combines these two estimation methods.

In the literature of estimation of half-lives of real exchange rates, the first order autoregressions of real exchange rates have been typically estimated by univariate methods. When a univariate method is combined with Hansen and Sargent's method as in our system method, then the system method estimator for the autoregressive coefficient is more efficient than the univariate method estimator as long as the linear rational expectations model is correctly specified. When the linear rational expectations model used in this paper is misspecified, the system method estimator is inconsistent. However, if the model is a good approximation, then the estimator's mean may be close to the true value and its variance may be much smaller than the univariate estimators.

In this paper, we are interested in the difference of half-lives of real exchange rates based on traded and non-traded good prices. The half-lives of the real exchange rates based on traded good price indices are expected to be shorter than those based on non-traded good or general price indices. An extreme case of this proposition is that the half-lives of the real exchange rates on traded good price indices are finite because the real exchange rates are stationary, but the half-lives of the real exchange rates based on

non-traded and general price indices are infinite because these real exchange rates are nonstationary.

The empirical evidence is mixed for this extreme view. Engel (1999) used a variance decomposition method to find how much variation in the real exchange rate can be explained by the variance in the relative price of the non-traded and traded goods. Under the extreme view, the relative price component will explain 100 percent of the real exchange rate volatility in the long run. Engel uses several measures of the traded good prices including PPI, and find no evidence that the relative price component explains most of the real exchange rate volatility at any time horizon he tries. In contrast, Kakkar and Ogaki (1999) used the WPI, CPI, and GDP implicit deflator as traded, non-traded, and general prices, and found empirical evidence that is consistent with the view that the real exchange rate based on PPI is stationary. Kim (1990) and Ito (1997) also found more favorable evidence for long-run PPP for WPI based real exchange rate than for CPI based real exchange rate.

One interpretation for these mixed results is that Engel's variance decomposition method is not very informative for long-run horizons because his method is designed to be applicable for both short-run and long-run horizons unlike Kakkar and Ogaki's (1999) and Kim's (1990) long-run methods. In this paper, we consider a less extreme view of shorter half-lives for real exchange rates based on traded good price indices compared with those for real exchange rates based on non-traded good and general price indices.

In this paper, we estimate half-lives of real exchange rates based on PPI, CPI, and GDP implicit deflator. Even though it is ideal to have pure traded and non-traded good price indices that cover all goods for our empirical work, it is very impossible to

find such price indices. For example, there is a non-traded component in an imported car price because of domestic retailing service. Service consumption is often treated as non-traded, but some types of legal services are traded across borders. The idea behind our use of CPI, PPI, and GDP implicit deflator is that the traded good component of the producer price index is proportionately larger than that of that of the consumer price index and the GDP implicit deflator. If the convergence rate is faster for traded good prices than that for non-traded good prices, half-lives for the real exchange rate based on the producer price index should be shorter than those for the real exchange rate based on the consumer price index and that on the GDP implicit deflator. Because non-traded good components are considered to be important in consumer goods compared with producer goods, the PPI and the Wholesale Price Index (WPI) have been also used as a traded good price index in the PPP literature (see, e.g., Kakkar and Ogaki, 1999).

Kim (2003) applied the same method as in this paper to a different data set. Kim followed Stockman and Tesar (1995) and used the implicit deflators of non-service consumption and service consumption classified by type and total consumption deflators to construct the real exchange rate for traded, non-traded, and general prices, respectively. The countries used in his study of bilateral exchange rates were Canada, France, Italy, Japan, Sweden, the United Kingdom and the United States. Kim used each of the seven currencies alternatively as the base currency in his empirical work.

In the exchange rate model we consider, there are two goods. The only conditions required for the model is that the long-run PPP holds for one of the goods, and that the two goods cover all the goods relevant for the money demand. Therefore, we do not need a pure tradable and non-tradable price indices for our empirical work.

The seven countries included in our study are Canada, France, Germany, Italy, Japan, the United Kingdom and the United States. It is of interest to use different measures of traded and non-traded good prices. Moreover, Kim's data set does not include Germany because the data are not available. Therefore, it is of interest to compare our results with Kim's. When the system method is applied, our point estimates indicate shorter half-lives for PPI than for CPI and GDP implicit deflators. This result is consistent with Kim's (2003).

## 2. An Exchange Rate Model with Sticky Prices

### 2.1. The Gradual Adjustment Equation

Let  $p_t^T$  be the log domestic traded goods price level,  $p_t^{T*}$  be the log foreign traded goods price level, and  $e_t$  be the log nominal exchange rate. We assume that the three variables,  $p_t^T$ ,  $p_t^{T*}$  and  $e_t$  are first difference stationary and that PPP holds in the long run, so that the real exchange rate defined by  $p_t^T - p_t^{T*} - e_t$  is stationary, or  $\mathbf{y}_t = (p_t^T, p_t^{T*}, e_t)'$  is cointegrated with a cointegrating vector  $(1, -1, -1)$ . Let  $\mu = E[p_t^T - p_t^{T*} - e_t]$ , then  $\mu$  can be nonzero when different units are used to measure the price levels in the two countries.

To derive the form of a structural ECM, we consider an exchange rate model with sticky prices. We employ Mussa's (1982) model, which may be viewed as a stochastic discrete time version of Dornbush's (1976) model, in which the domestic price of traded goods is assumed to be sticky in the short run and to adjust gradually to its long-run equilibrium level determined by PPP with rational expectations.



Employing Mussa's (1982) model, the domestic price of traded goods is assumed to be sticky in the short run and to adjust gradually to its equilibrium level in the long run through

$$\Delta p_{t+1}^T = b[\mu + p_t^{T*} + e_t - p_t^T] + E[p_{t+1}^{T*} + e_{t+1} | I_t] - [p_t^{T*} + e_t] \quad (1)$$

where  $\Delta x_{t+1} = x_{t+1} - x_t$  for any variable  $x_t$ ,  $E[\cdot | I_t]$  is the expectation operator conditional on the information,  $I_t$ , available to the economic agents at time  $t$ , and  $b$  is a short-run adjustment coefficient which is a positive constant,  $b < 1$ . Based on Mussa (1982), the main idea behind equation (1) is that the price level of domestic traded goods adjusts slowly toward its long-run PPP level (i.e. long-run equilibrium level) of  $p_t^{T*} + e_t$ . The short-run adjustment speed is slow when  $b$  is close to zero, and the adjustment speed is fast when  $b$  is close to one. From equation (1), we have

$$\Delta p_{t+1}^T = d + b[p_t^{T*} + e_t - p_t^T] + \Delta p_{t+1}^{T*} + \Delta e_{t+1} + \varepsilon_{t+1} \quad (2)$$

where  $d = b\mu$ , and  $\varepsilon_{t+1} = E[p_{t+1}^{T*} + e_{t+1}] - [p_{t+1}^{T*} + e_{t+1}]$ . Thus  $\varepsilon_{t+1}$  is a one period ahead forecasting error, and  $E[\varepsilon_{t+1} | I_t] = 0$ . Equation (2) motivates the form of the structural ECM employed in this paper and it can be referred as the structural gradual adjustment equation. In the application of this paper, the gradual adjustment equation implies the first order autoregression structure for the real exchange rate defined by traded good prices. To see this, let  $s_t = p_t^{T*} + e_t - p_t^T$  be the log real exchange rate. Then equation (2) implies

$$s_{t+1} = -d + (1-b)s_t - \varepsilon_{t+1}. \quad (3)$$

We define the half-life of the log real exchange rate as the number of periods required for a unit shock to dissipate by one half in this first order autoregression.

## 2.2. The Exchange Rate under Rational Expectations

In order to obtain a solution for the nominal exchange rate and the domestic traded good in terms of other variables, we now consider the money demand equation and the Uncovered Interest Parity condition. The money demand depends on the general price level rather than the traded good price. The general price level is assumed to be a weighted average of the prices of the traded and non-traded goods. Let

$$P_t = (1-\alpha) p_t^T + \alpha p_t^N \quad (4)$$

$$P_t^* = (1-\alpha^*) p_t^{T*} + \alpha^* p_t^{N*} \quad (5)$$

$$m_t = k + P_t - h i_t \quad (6)$$

$$i_t = i_t^* + E[e_{t+1} | I_t] - e_t \quad (7)$$

where  $p_t^N$  is the log of the price of non-traded goods and  $p_t^T$  is the log of the price of traded goods with weights  $\alpha$  and  $(1-\alpha)$ , respectively. The  $m_t$  is the log nominal money supply minus the log real national income,  $i_t$  is the nominal interest rate in the domestic country, and  $i_t^*$  is the nominal interest rate in the foreign country. In (6), we are assuming that the income elasticity of money demand is one. From (4), (5), (6) and (7), we obtain

$$E[e_{t+1} | I_t] - e_t = (1/h)[(1-\alpha)p_t^T - \omega - h(1-\alpha)\{E[p_{t+1}^{T*} - p_t^{T*} | I_t]\}] \quad (8)$$

where  $\omega = m_t - k + h r_t^* + \alpha p_t^N$  and  $r_t^* = i_t^* - (1-\alpha^*)\{E[p_{t+1}^{T*} | I_t] - p_t^{T*}\}$

Following Mussa, solving (1) and (8) as a system of stochastic difference equations for  $E[p_{t+j}^T | I_t]$  and  $E[e_{t+j} | I_t]$  for a fixed  $t$  yields

$$p_t^T = E[F_t | I_{t-1}] - \sum_{j=1}^{\infty} (1-b)^j \{E[F_{t-j} | I_{t-j}] - E[F_{t-j} | I_{t-j-1}]\} \quad (9)$$

$$e_t = \frac{bh + (1-\alpha)}{bh} E[F_t | I_t] - p_t^{T*} - \frac{(1-\alpha)}{bh} p_t^T \quad (10)$$

where

$$F_t = (1-\delta) \sum_{j=0}^{\infty} \delta^j \psi_{t+j} \quad (11)$$

$$\delta = h / (h + 1 - \alpha) \text{ and}$$

$$\psi_{t+j} = m_t - k - h r_t^* + \alpha p_t^{T*} + h \alpha^* \{E[p_{t+j}^{T*} / I_t] - p_t^{T*}\} \quad (12)$$

$$r_t^* = i_t^* - (1-\alpha^*) \{E[p_{t+1}^{T*} / I_t] - p_t^{T*}\}$$

We assume that  $\psi(t)$  is first difference stationary. Since  $\delta$  is a positive constant smaller than one, this implies that  $F_t$  is also first difference stationary. From (9) and (10),

$$e_t + p_t^{T*} - p_t^T = \frac{bh + (1-\alpha)}{bh} \sum_{j=1}^{\infty} (1-b)^j \{E[F_{t-j} | I_{t-j}] - E[F_{t-j} | I_{t-j-1}]\} \quad (13)$$

Since the right hand side of (13) is stationary<sup>1</sup>,  $e_t + p_t^{T*} - p_t^T$  is stationary. Thus, equation (13) implies that  $(p_t^T, e_t, p_t^{T*})$  is cointegrated, with the cointegrating vector  $(1, -1, -1)$ .

### 2.3. Hansen and Sargent's Formula

In this paper, Hansen and Sargent's (1980, 1982) formula for linear rational expectations models is employed to obtain a structural ECM representation from the exchange rate model. From (10), we obtain

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<sup>1</sup> This assumes that  $E_t[F_t] - E_{t-1}[F_t]$  is stationary, which is true for a large class of first difference stationary variable  $F_t$  and information sets.

$$\Delta e_{t+1} = \frac{bh + (1-\alpha)}{bh} (1-\delta) E \left[ \sum_{j=0}^{\infty} \delta^j \Delta \psi_{t+j+1} \mid I_t \right] - \frac{(1-\alpha)}{bh} \Delta p_{t+1}^T - \Delta p_{t+1}^{T*} + \varepsilon_{e,t+1} \quad (14)$$

where  $\varepsilon_{e,t+1} = \frac{bh + (1-\alpha)}{bh} \{E[F_{t+1} \mid I_{t+1}] - E[F_{t+1} \mid I_t]\}$ , so that the law of iterated expectations implies  $E[\varepsilon_{e,t+1} \mid I_t] = 0$ . Because this equation involves a discounted sum of expected future values of  $\Delta \psi_t$ , the system method using Hansen and Sargent's (1982) method is applicable.

Hansen and Sargent (1982) propose to project the conditional expectation of the discounted sum,  $E[\sum \delta^j \Delta \psi_{t+j+1} \mid I_t]$ , onto an information set  $H_t$ , the econometrician's information set at  $t$ , which is a subset of  $I_t$ , the economic agents' information set. Let  $\hat{E}[\cdot \mid H_t]$  be the linear projection operator, conditional on the information set  $H_t$ .

We take the econometrician's information set at  $t$ ,  $H_t$ , to be the one generated by linear functions of the current and past values of  $\Delta p_t^{T*}$ . Then, replacing the best forecast of the economic agents,  $E[\sum \delta^j \Delta \psi_{t+j+1} \mid I_t]$  by the econometrician's linear forecast based on  $H_t$  in equation (14), we obtain

$$\Delta e_{t+1} = \frac{bh + (1-\alpha)}{bh} (1-\delta) \hat{E} \left[ \sum_{j=0}^{\infty} \delta^j \Delta \psi_{t+j+1} \mid H_t \right] - \frac{(1-\alpha)}{bh} \Delta p_{t+1}^T - \Delta p_{t+1}^{T*} + u_{2,t+1} \quad (15)$$

where

$$u_{2,t+1} = \varepsilon_{e,t+1} + \frac{bh + (1-\alpha)}{bh} (1-\delta) \{E[\sum \delta^j \Delta \psi_{t+j+1} \mid I_t] - \hat{E}[\sum \delta^j \Delta \psi_{t+j+1} \mid H_t]\}$$

Because  $H_t$  is a subset of  $I_t$ , we obtain  $\hat{E}[u_{2,t+1} \mid H_t] = 0$ .

Since  $\hat{E}[\cdot \mid H_t]$  is the linear projection operator onto  $H_t$ , there exist possibly infinite order lag polynomials  $\beta(L)$ ,  $\gamma(L)$ , and  $\xi(L)$ , such that

$$\hat{E}[\Delta p_{t+1}^{T*} | H_t] = \beta(L) \Delta p_t^{T*} \quad (16)$$

$$\hat{E}[\Delta \psi_{t+1} | H_t] = \gamma(L) \Delta p_t^{T*} \quad (17)$$

$$\hat{E}\left[\sum_{j=0}^{\infty} \delta^j \Delta \psi_{t+j+1} | H_t\right] = \xi(L) \Delta p_t^{T*} \quad (18)$$

Then, following Hansen and Sargent (1980, Appendix A), we obtain the restrictions imposed by (15) on  $\xi(L)$ :

$$\xi(L) = \frac{\gamma(L) - \delta L^{-1} \gamma(\delta) \{1 - \delta \beta(\delta)\}^{-1} \{1 - L \beta(L)\}}{1 - \delta L^{-1}} \quad (19)$$

Assume that linear projections of  $\Delta p_{t+1}^{T*}$  and  $\Delta \psi_{t+1}$  onto  $H_t$  have only a finite number of  $\Delta p_t^{T*}$  terms:

$$\hat{E}[\Delta p_{t+1}^{T*} | H_t] = \beta_1 \Delta p_t^{T*} + \beta_2 \Delta p_{t-1}^{T*} + \dots + \beta_p \Delta p_{t-p+1}^{T*} \quad (20)$$

$$\hat{E}[\Delta \psi_{t+1} | H_t] = \gamma_1 \Delta p_t^{T*} + \gamma_2 \Delta p_{t-1}^{T*} + \dots + \gamma_{p-1} \Delta p_{t-p+2}^{T*} \quad (21)$$

Here, we assume  $\beta(L)$  is of order  $p$  and  $\gamma(L)$  is of order  $p-1$  in order to simplify the exposition, but we do not lose generality because any  $\beta_i$  and  $\gamma_i$  can be zero. Then, as in Hansen and Sargent (1982), (19) implies that  $\xi(L) = \xi_0 + \xi_1 L + \dots + \xi_p L^p$ , where

$$\begin{aligned} \xi_0 &= \gamma(\delta) \{1 - \delta \beta(\delta)\}^{-1} \\ \xi_j &= \delta \gamma(\delta) \{1 - \delta \beta(\delta)\}^{-1} (\beta_{j+1} + \delta \beta_{j+2} + \dots + \delta^{p-j} \beta_p) \\ &\quad + (\gamma_j + \delta \gamma_{j+1} + \dots + \delta^{p-j} \gamma_p) \end{aligned} \quad (22)$$

for  $j = 1, \dots, p$ .

Then,

$$\hat{E} \left[ \sum_{j=0}^{\infty} \delta^j \Delta \psi_{t+j+1} \mid H_t \right] = \xi_1 \Delta p_t^{T*} + \xi_2 \Delta p_{t-1}^{T*} + \dots + \xi_p \Delta p_{t-p+1}^{T*} \quad (23)$$

Combining (2), (15), (20), and (21) with (23), we obtain a system of four equations:

$$\Delta p_{t+1}^T = d + \Delta p_{t+1}^{T*} + \Delta e_{t+1} - b [p_t^T - p_t^{T*} - e_t] + u_{1,t+1} \quad (24)$$

$$\Delta e_{t+1} = -\frac{(1-\alpha)}{bh} \Delta p_t^T - \Delta p_t^{T*} + \mu \xi_1 \Delta p_t^{T*} + \mu \xi_2 \Delta p_{t-1}^{T*} + \dots + \mu \xi_p \Delta p_{t-p+1}^{T*} + u_{2,t+1} \quad (25)$$

$$\Delta p_{t+1}^{T*} = \beta_1 \Delta p_t^{T*} + \beta_2 \Delta p_{t-1}^{T*} + \dots + \beta_p \Delta p_{t-p+1}^{T*} + u_{3,t+1} \quad (26)$$

$$\Delta \psi_{t+1} = \gamma_1 \Delta p_t^{T*} + \gamma_2 \Delta p_{t-1}^{T*} + \dots + \gamma_{p-1} \Delta p_{t-p+2}^{T*} + u_{4,t+1} \quad (27)$$

where  $\mu = \frac{bh + (1-\alpha)}{bh} (1-\delta)$ , and  $u_{1,t+1} = \varepsilon_{t+1}$ .

Given the data for  $[\Delta p_{t+1}^T, \Delta e_{t+1}, \Delta p_{t+1}^{T*}, \Delta \psi_{t+1}]'$ , the system method can be applied to these four equations. There exist additional complications for obtaining data for  $\Delta \psi_{t+1}$ , which will be discussed later in this paper.

### 3. Structural Models and Error Correction Models

Let  $\mathbf{Y}_t$  be a  $n$ -dimensional vector of first difference stationary random variables, and assume that there exists  $\rho$  linearly independent cointegrating vectors, so that  $\mathbf{A}'\mathbf{Y}_t$  is stationary, where  $\mathbf{A}'$  is a  $(\rho \times n)$  matrix of real numbers whose rows are linearly independent cointegrating vectors.

Consider a standard ECM.

$$\Delta \mathbf{Y}_{t+1} = \mathbf{k} + \mathbf{Q}\mathbf{A}'\mathbf{Y}_t + \mathbf{F}_1 \Delta \mathbf{Y}_t + \mathbf{F}_2 \Delta \mathbf{Y}_{t-1} + \dots + \mathbf{F}_p \Delta \mathbf{Y}_{t-p+1} + \mathbf{v}_{t+1} \quad (28)$$

where  $\mathbf{k}$  is an  $(n \times 1)$  vector,  $\mathbf{Q}$  is an  $(n \times \rho)$  matrix of real numbers, and  $\mathbf{v}_t$  is a stationary  $n$ -dimensional vector of random variables with  $\hat{E}[\mathbf{v}_{t+1}|H_t]=0$ .

A class of structural models can be written in the following form of a structural ECM:

$$\mathbf{C}_0 \Delta \mathbf{Y}_{t+1} = \mathbf{d} + \mathbf{B} \mathbf{A}' \mathbf{Y}_t + \mathbf{C}_1 \Delta \mathbf{Y}_t + \mathbf{C}_2 \Delta \mathbf{Y}_{t-1} + \dots + \mathbf{C}_p \Delta \mathbf{Y}_{t-p+1} + \mathbf{u}_{t+1} \quad (29)$$

where  $\mathbf{C}_i$  is a  $(n \times n)$  matrix,  $\mathbf{d}$  is a  $(n \times 1)$  vector, and  $\mathbf{B}$  is a  $(n \times \rho)$  matrix of real numbers. Here,  $\mathbf{C}_0$  is a nonsingular matrix of real numbers with ones along its principal diagonal, and  $\mathbf{u}_t$  is a stationary  $n$ -dimensional vector of random variables with  $\hat{E}[\mathbf{u}_{t+1}|H_t] = 0$ . Even though the cointegrating vectors are not unique, we assume that there is a normalization that uniquely determines  $\mathbf{A}$ , so that parameters in  $\mathbf{B}$  have structural meanings.

The exchange rate model with sticky price can be written in the structural ECM form (29) as in the system of four equations (24)-(27): we have  $\mathbf{y}_t = [\Delta p_{t+1}^T, \Delta e_{t+1},$

$$\Delta p_{t+1}^{T*}, \Delta \psi_{t+1}]', \mathbf{B} = [-b, 0, 0, 0]', \mathbf{A} = [1, -1, -1, 0]',$$

$$\mathbf{C}_0 = \begin{bmatrix} 1 & -1 & -1 & 0 \\ (1-\alpha)/bh & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (30)$$

and

$$\mathbf{C}_j = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & \mu \xi_j & 0 \\ 0 & 0 & \beta_j & 0 \\ 0 & 0 & \gamma_j & 0 \end{bmatrix} \quad (31)$$

for  $j = 1, \dots, p$

Comparing equation (28) with equation (29), in many applications of standard ECMs given in equation (28), elements in  $\mathbf{Q}$  are given structural interpretations as parameters of the speed of adjustment toward the long-run equilibrium represented by  $\mathbf{A}'\mathbf{Y}_t$ . However, if we assume that in equation (29)  $\mathbf{C}_0$  is nonsingular, and pre-multiply both sides of (29) by  $\mathbf{C}_0^{-1}$ , we obtain the standard ECM given in equation (28), where  $\mathbf{k} = \mathbf{C}_0^{-1}\mathbf{d}$ ,  $\mathbf{Q} = \mathbf{C}_0^{-1}\mathbf{B}$ ,  $\mathbf{F}_i = \mathbf{C}_0^{-1}\mathbf{C}_i$ , and  $\mathbf{v}_t = \mathbf{C}_0^{-1}\mathbf{u}_t$ . Thus, the standard ECM, estimated by Engle and Granger's (1987) two step method or Johansen's (1988) Maximum Likelihood method, is a reduced form model. Hence, it cannot be used to recover structural parameters in  $\mathbf{B}$ , nor can the impulse response functions based on  $\mathbf{v}_t$  be interpreted in a structural way, unless some restrictions are imposed on  $\mathbf{C}_0$ .

As in a VAR, various restrictions are possible for  $\mathbf{C}_0$ . One example is to assume that  $\mathbf{C}_0$  is lower triangular. If  $\mathbf{C}_0$  is lower triangular, then the first row of  $\mathbf{Q}$  in equation (28) is equal to the first row of  $\mathbf{B}$  in equation (29), and structural parameters in the first row of  $\mathbf{B}$  are estimated by the standard methods to estimate an ECM.

However, in the exchange rate model we present in this paper, we are interested in  $b$  that represents a structural parameter. In estimating  $b$  in the model, the restriction that  $\mathbf{C}_0$  in equation (29) is lower triangular is not attractive. As we can see from equation (30), the structural ECM from the two-good version of the exchange rate model does not satisfy the restriction that  $\mathbf{C}_0$  is lower triangular for any ordering of the variables.

Based on equation (30), we can see the relationship between the structural ECM and the reduced form ECM in the exchange rate model. Because



$$\mathbf{C}_0^{-1} = \begin{bmatrix} \frac{bh}{bh+(1-\alpha)} & \frac{bh}{bh+(1-\alpha)} & 0 & 0 \\ \frac{(1-\alpha)}{bh+(1-\alpha)} & \frac{bh}{bh+(1-\alpha)} & -1 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (32)$$

$\mathbf{Q} = \mathbf{C}_0^{-1} \mathbf{B} = [-b^2h/(bh+(1-\alpha)), b(1-\alpha)/(bh+(1-\alpha)), 0, 0]'$  in the reduced form model, and  $\mathbf{B} = [-b, 0, 0, 0]'$  in equation (7). The speed of adjustment coefficient for the domestic price is  $b$  in the structural model, while it is  $b^2h/[bh+(1-\alpha)]$  in the reduced form model. The error correction term does not appear in the second equation for the exchange rate in the structural ECM, while it appears with the speed of adjustment coefficient of  $b(1-\alpha)/[bh+(1-\alpha)]$  in the reduced form model.

#### 4. The System Method

In order to implement the system method, we need data for  $\Delta\psi_t$ , which requires knowledge of  $\alpha$  and  $h$ . In order to compute  $\alpha$ , weights on the non-traded goods, we followed Kakkar and Ogaki (1999). We applied a cointegrating regression of log real exchange rate defined by GDP implicit deflator onto log relative price in Japan and log relative price in a foreign country to estimate  $\alpha$  and  $\alpha^*$ .<sup>2</sup> For  $h$ , even though  $h$  is unknown, a cointegrating regression can be applied to money demand if money demand is stable in the long-run, as in Stock and Watson (1993). For this purpose, we augment the model as follows:

$$m_t = k + P_t - hi_t + \eta_{m,t} \quad (33)$$

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<sup>2</sup> Here, the relative price is CPI/PPI. See Kakkar and Ogaki (1999) for details.

where  $\eta_{m,t}$  is the money demand shock, which is assumed to be stationary, so that money demand is stable.

By redefining  $m_t$  as  $m_t - \eta_{m,t}$ , the same equations as those in section two are obtained. For the measurement of  $\Delta\psi_t$ , note that the *ex ante* foreign real interest rate can be replaced by the *ex post* foreign real exchange rate because of the Law of Iterated Expectations. Using the money market clearing condition (33) and (12), we obtain

$$\Delta\psi_{t+1} = \Delta P_{t+1} - h\Delta i_{t+1} + h\Delta i_{t+1}^* + \alpha\Delta p_{t+1}^N - h(1-2\alpha^*)[\Delta p_{t+2}^{T*} - \Delta p_{t+1}^{T*}] \quad (34)$$

Hence, when  $h$ ,  $\alpha$ , and  $\alpha^*$  are obtained,  $\Delta\psi_t$  can be obtained from the prices of traded and non-traded goods and interest rate data without data for monetary aggregate and national income.

We have now obtained a system of four equations (24), (25), (26), and (27). Because  $E[u_{1,t}/I_t] = 0$ , we can choose instrument variables,  $z_{1,t}$ , for  $u_{1,t}$  from  $I_t$  and, since  $\hat{E}[u_{i,t}/H_t] = 0$ , instrumental variables,  $z_{i,t}$ , for  $u_{i,t}$  can be selected from  $H_t$  for  $i = 2, 3, 4$ .

Because the speed of adjustment,  $b$ , for  $p_t^T$  affects the dynamics of the other variables<sup>3</sup>, there are cross-equation restrictions involving  $b$  in many applications to the restrictions in (22). Using the moment conditions  $E[z_{i,t}u_{i,t}] = 0$  for  $i = 1, \dots, 4$ , we form a GMM estimator, imposing the restrictions from (22) and the other cross-equation restrictions implied by the model.

Given the cointegrating vector, this system method provides more efficient estimators than the single equation method, as long as the restrictions implied by the

model are true. On the other hand, the single equation method estimators are more robust because misspecification in the other equations does not affect their consistency. The cross-equation restrictions can be tested by Wald, Likelihood Ratio type, and Lagrange Multiplier tests in a GMM framework (e.g., see Ogaki (1993a)). When the restrictions are nonlinear, Likelihood Ratio type and Lagrange Multiplier tests are known to be more reliable than Wald tests.

## 5. Empirical Results

In this paper, we use each of the seven currencies alternatively as the base currency. We use PPI, CPI, and the GDP implicit deflators from 1973 Q1 to 2001 Q1 to construct the real exchange rates. The countries are Canada, France, Germany, Italy, Japan, the United Kingdom and the United States. Both CPI and PPI are from the OECD Main Economic Indicators. For the PPI, we use Manufacturing Industry Products in Domestic Wholesale Price Index for Japan, Manufacturing output price for Germany, and Home market (excluding VAT) for Italy, and Domestic market (excluding food, beverages, and tobacco and petroleum) for United Kingdom. For the GDP implicit deflator, we use data from the OECD Main Economic Indicators except for Japan and Germany. For Japan, the data are obtained from the National Accounts published by the Cabinet Office of the Government of Japan are used. For Germany, the data published by the Bundesbank are obtained from the Data Stream. Monthly average foreign exchange rates with U.S. dollar as the base currency from the OECD Main Economic Indicators. In order to estimate the interest elasticity of money

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<sup>3</sup> Note that only  $p_i^T$  adjusts slowly, but  $b$  affects the dynamics of other variables because of interactions of  $p_i^T$  with those variables.

demand, we use the sum of M1 and Quasi Money as the measure of M2 as the IFS suggests. The three-month T-bill rates are used for the interest rate data, but for Japan three-month deposit rates are employed because Japanese T-bill rates are not available in an early part of the sample.

In the present study, the estimation procedure has two steps. First, we estimate the monetary equilibrium equation using Park's (1992) Canonical Cointegrating Regression (CCR) to obtain the interest elasticity of money demand. Second, the speed of price adjustment is estimated by applying GMM to the structural ECM.

Tables 1 and 2 present the results of cointegrating regression for the money demand equations of the GDP implicit deflator and the weights on the non-traded goods,  $\alpha$  and  $\alpha^*$ , for each country. We report the third stage estimates of CCR for the coefficients and the fourth stage test results. In Table 1, the deterministic cointegrating restrictions are not rejected for most countries except U.K. and Japan, and the null of stochastic cointegration is not rejected for most countries with the exception of Canada, Germany, and Japan at the 5 % level of significance. To compute  $\alpha$  and  $\alpha^*$  in Table 2, weights on the CPI, we followed Kakkar and Ogaki (1999). The results in Table 2 show that we have not only theoretically correct signs but also the theoretically correct magnitudes for most countries except Italy whose weight on CPI has the theoretically incorrect sign. Furthermore, the deterministic cointegration restriction and the stochastic cointegration are not rejected at the five percent level for each country.

Tables 3, 4, and 5 report the results of GMM estimation for PPI, CPI and GDP implicit deflators using the system method, equations (24)~(27).<sup>4</sup> We also report the

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<sup>4</sup> For the results of GDP implicit deflators (general prices), we used the system method of Kim, Ogaki, and Yang (2003) for a single-good model.

estimation results with additional sample period, namely 1973:Q1~1990:Q2, to see if German Economic and Monetary Union affects our results. The instrumental variables are  $\Delta p_{t-3}^{T*}$  and  $\Delta p_{t-4}^{T*}$ , which are foreign traded goods prices in all cases.<sup>5</sup> For each country, the estimation results are reported under the assumption that PPP holds in the long run. In the system method, the structural speed of the adjustment coefficient,  $b$ , appears in two equations: the gradual adjustment equation, (24), and the Hansen-Sargent equation, (27). The model imposes the restriction that the coefficient  $b$  in the gradual adjustment equation is the same as the coefficient  $b$  in the Hansen-Sargent equation. We report results with and without this restriction imposed for the system method of estimation. In the case of unrestricted estimation,  $b_{u,hs}$  is the estimate of  $b$  from Hansen-Sargent equation, and  $b_{u,ga}$  is the estimate of  $b$  from the gradual adjustment equation. The restricted estimate is denoted by  $b_r$ . The likelihood ratio type test statistic denoted by LR is used to test the restriction. In most cases, this restriction is not rejected at the 5 % level. Furthermore, for the test of the Hansen-Sargent restrictions we also report the likelihood ratio type test statistic, denoted by LR1.<sup>6</sup> For all cases the null hypothesis is not rejected at the ten percent level, which is evidence in favor of the Hansen-Sargent restrictions are satisfied.

To obtain the half-life estimate, we use the restricted estimate of the structural speed of the adjustment coefficient,  $b$ , in each case. Because  $1-b$  is the AR coefficient for the first order AR representation as in equation (3), and because our data are quarterly, the half life is calculated as  $0.25 \ln(0.5)/\ln(1-b)$ . All restricted estimates for

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<sup>5</sup> The selection of the instrumental variables is based on Akaike Information Criteria (AIC).

<sup>6</sup> This test is done by conducting the likelihood ratio type test comparing the J statistics with the Hansen-Sargent restriction from the linear rational expectations model and unrestricted one with free parameters.

the structural speed of the adjustment coefficient have the theoretically correct positive sign. Furthermore, most of them are significant at the five percent level.

The results in Tables 3 show that the estimated half-lives of the PPI-based real exchange rates range from 0.08 to 0.99 year. All half-life estimates are shorter than one year and much shorter than the consensus of 3-5 years explained by Rogoff (1996) and others.<sup>7</sup> For the GDP implicit deflator-based real exchange rates in Table 5, the estimated half-lives range from 0.16 to 1.48 years. For the CPI-based real exchange rates in Table 4, the half-life estimates fall in the 0.20- to 2.95-year range. When comparing to the adjustment speeds over the full samples to those for subsamples, the results are not very different for the full sample and the subsample.

In most cases, the point estimate for the half-life of the GDP implicit deflator-based real exchange rate is larger than that of the PPI-based real exchange rate and is smaller than of the CPI-based real exchange rate for each pair of countries. Similarly, in most cases, the standard error for the half-life of the GDP implicit deflator-based real exchange rate is larger than that of the PPI-based real exchange rate, and is smaller than that of the CPI-based real exchange rate.

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<sup>7</sup> Frankel (1986) uses a 116 year long data for the WPI based dollar/pound real exchange rate and reports a half-life of 4.6 years. Abuaf and Jorian (1990) use Lee (1976) data for WPI based real exchange rates for the US and 8 countries report 3.3 years of half-lives, Glen (1992) and Cheung and Lai (1994) find similar results with the data. Lothian and Taylor (1996) use two centuries of data for the dollar-pound rate and the franc-pound rate, and found half-life of 4.7 and 2.5 years, respectively. Diebold, Husted, and Rush (1991), using data for the gold standard period, find average half-life of 2.8 years.

## 6. Conclusions

In this paper, we used a system method based on a structural ECM to estimate half-lives of PPI-, CPI-, and GDP implicit deflator-based real exchange rates for G7 countries. The empirical results in this paper can be summarized in three ways. First, our results indicate that the system method based on a structural ECM provide uniformly shorter half-lives than the consensus of 3-5 years explained by Rogoff (1996). They also show that all of our half-life estimates for the PPI-based real exchange rates are less than one year. For each country, the point estimate for the half-life of the GDP implicit deflator-based real exchange rate is larger than that of the PPI-based real exchange rate and is smaller than of the CPI-based real exchange rate. Even for the CPI-based real exchange rate, our estimates of the half-lives range from 0.20 to 2.95 years.

Some recent studies, using producer price indices and tradable sector deflators, which apply panel unit root tests to real exchange rates, report strong evidence against the unit root null and estimate the half-life of PPP deviation to be 3-5 years.<sup>8</sup> Note that, even for the rates of traded goods, this remarkable consensus of 3-5 year half-life is the same as that found for real exchange rates for general prices in many studies. These studies that attempt to solve the PPP puzzle of the 3-5 year half-life typically conduct Dickey-Fuller or Augmented Dickey-Fuller regression, and the half-life is calculated

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<sup>8</sup> Wu (1996) uses quarterly CPI and WPI, and report half-life of around 2.5 years. Parsley and Wei (1996) use the tradable sector deflator and find that half-life of PPP deviation is still 4-5 years. Chinn and Johnston (1996) employ CPI and estimate a cointegrating relationship, and the half-life of deviations from the equilibrium defined by the cointegrating vector is 4-5 years. Papell (1997, 2001), Fleissig and Strauss (2000), and Papell and Theodoridis (2001) find shorter half-lives of 2 to 2.5 years. Murray and Papell (2001) confirms Rogoff's original claim of 3-5 years.

from the coefficient of the lagged real exchange rate. However, this suggests that the point estimates and the empirical results from the univariate methods may not provide the structural interpretation of the adjustment speed and the half-life of PPP deviation.

Second, our results indicate that a sharper estimation of the half-life is possible when we use price indices with large traded good price components together with a system method for each country. This is because the standard error for the half-life of the GDP implicit deflator-based real exchange rate is larger than that of the PPI-based real exchange rate, and is smaller than that of the CPI-based real exchange rate.

Third, our estimates suggest that theories of international price determination should treat traded and non-traded goods differently to match their differential convergence rates. All of the European and other real exchange rates for PPI show that their half-lives tend to be shorter than those for GDP implicit deflator and CPI. These real exchange rates for PPI are among the most likely to exhibit evidence of short-run and long-run PPP, because trade between European countries as well as major trading partners has relatively low transaction costs and relatively stable non-tariff barriers to trade. This result is interesting, because it confirms that traded goods prices tend to adjust faster than general prices and non-traded goods' prices, implying shorter half-lives for PPI-based rates than for general prices and CPI-based rates. Moreover, it may be that traded good convergence rates are more plausible estimates of the impact of nominal rigidities while considerations such as international factor immobility and non-traded components of goods' prices are important for the dynamic behavior of the overall price index.

The non-traded good price component in the CPI is considered to be the largest and the traded good price component in the PPI is considered to be the largest among



the three price indices used in this paper. This observation readily explain our result that the half-life of the real exchange rate is the longest when the CPI is used, and is the shortest when the PPI is used. Our result is consistent with the results regarding long-run PPP in Kim (1990), Ito (1997), Kakkar and Ogaki (1999), and Kim (2003). Our result is in contrast with Engel's (1999) results that find no evidence for faster convergence to the PPP level for the PPI-based real exchange rates compared with the CPI-based real exchange rates. In the future work, we also plan to relax the UIP assumption. For example, in Lim and Ogaki's (2003) model, the UIP essentially holds for the long-term interest rate differential, but the forward premium anomaly exists for the short-term interest differential. It may be possible to develop a system method based on the UIP for the long-term interest rate differential.

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**Table 1. Money Demand Equation of GDP Implicit Deflator**

<b>Country</b>	<b>h<sup>a</sup></b>	<b>H(0, 1)<sup>b</sup></b>	<b>H(1, 2)<sup>c</sup></b>	<b>H(1, 3)<sup>d</sup></b>
Canada	25.0011 (9.2315)	0.0217 (0.8828)	9.5442 (0.0020)	14.2803 (0.0007)
France	14.5611 (3.6431)	2.5667 (0.1091)	1.9930 (0.1580)	3.0491 (0.2177)
Italy	25.6649 (9.7020)	3.1159 (0.7752)	1.7147 (0.1903)	1.9280 (0.3813)
Japan	6.125 (2.198)	5.071 (0.024)	4.160 (0.041)	10.787 (0.004)
Germany	18.7127 (4.7219)	3.6041 (0.0576)	5.5793 (0.0181)	8.9326 (0.0114)
U.K.	9.6147 (5.6209)	14.8621 (0.0001)	0.0923 (0.7612)	0.8609 (0.6501)
U.S.	49.9178 (15.8720)	0.0709 (0.7899)	2.2288 (0.1354)	2.4315 (0.2964)

Note: Results for  $m_t = k + P_t - h_i + \eta_{m,t}$

Column (a): Standard errors are in parenthesis

Column (b)-(d): P-values are in parenthesis.

**Table 2. Weight on CPI,  $\alpha$  and  $\alpha^*$** 

<b>Country</b>	<b><math>\alpha^a</math></b>	<b><math>\alpha^{*a}</math></b>	<b>H(0, 1)<sup>b</sup></b>	<b>H(1, 2)<sup>c</sup></b>	<b>H(1, 3)<sup>d</sup></b>
Canada	0.3794 (0.0825)	0.1558 (0.0518)	3.5560 (0.0593)	1.2379 (0.2658)	2.6892 (0.2606)
France	0.3222 (0.0748)	0.3545 (0.0489)	0.0051 (0.9425)	0.6855 (0.4076)	4.2166 (0.1214)
Italy	0.2177 (0.1329)	-0.2921 (0.1365)	0.9701 (0.3246)	0.9740 (0.3236)	1.9812 (0.3713)
Germany	0.6383 (0.0971)	0.0534 (0.1159)	3.0071 (0.0829)	3.8143 (0.0508)	5.2977 (0.0707)
U.K.	0.4492 (0.0470)	0.8129 (0.1069)	3.3913 (0.0655)	0.8517 (0.3560)	6.5428 (0.0379)
U.S.	0.1250 (0.0357)	0.4225 (0.0800)	1.8838 (0.1698)	0.4124 (0.5207)	0.7249 (0.6959)

Note: Results for  $s_t = \theta + \alpha q_t - \alpha^* q_t^* + \xi_t$  where  $s_t$  is log real exchange rate defined GDP implicit deflator,  $q_t$  is CPI/PPI in Japan and  $q_t^*$  is CPI/PPI in foreign country.

Column (a): Standard errors are in parenthesis

Column (b)-(d): P-values are in parenthesis.

**Table 3. The System Method Results for PPI-based Real Exchange Rates**

<b>Currencies</b>	<b>Half-life (a)</b>	<b><math>b_r</math> (b)</b>	<b><math>J_r</math> (c)</b>	<b><math>b_{u,hs}</math> (d)</b>	<b><math>b_{u,ga}</math> (e)</b>	<b><math>J_u</math> (f)</b>	<b>LR (g)</b>	<b>LR1 (h)</b>
US/JP	0.37 (0.0741)	0.3702 (0.0423)	7.2969 (0.1210)	1296.3 (94200)	0.2363 (0.1900)	7.0414 (0.0516)	0.2555 (0.6132)	1.4913 (0.4744)
UK/JP	0.28 (0.1281)	0.4655 (0.1818)	5.1995 (0.2674)	-0.0754 (0.6702)	1.1210 (0.5284)	2.7345 (0.4344)	2.4650 (0.1164)	4.2922 (0.1169)
CA/JP	0.41 (0.2186)	0.3427 (0.0932)	2.5427 (0.6370)	-1.2754 (0.7582)	0.2012 (0.2313)	1.8432 (0.6055)	0.6995 (0.4029)	0.1539 (0.9259)
FR/JP	0.90 (0.1438)	0.1749 (0.0059)	2.7932 (0.5930)	0.1295 (0.1594)	0.1933 (0.2314)	1.9487 (0.5832)	0.8445 (0.3581)	1.4011 (0.4963)
GE/JP	0.30 (0.1084)	0.4428 (0.1252)	2.0862 (0.7199)	0.1237 (0.1252)	0.4327 (0.4404)	1.8297 (0.6084)	0.2565 (0.6125)	0.0966 (0.9528)
(73:I~90:II)	0.26 (0.0670)	0.4882 (0.1163)	1.7985 (0.7727)	0.3890 (0.2097)	0.9866 (0.4895)	0.4016 (0.9398)	1.3969 (0.2372)	0.0585 (0.9711)
IT/JP	0.44 (0.4163)	0.3247 (0.1454)	1.2565 (0.8687)	1245.3 (32196)	0.1638 (0.1298)	1.1665 (0.7610)	0.0900 (0.7641)	0.0411 (0.9796)
UK/US	0.25 (0.0621)	0.4969 (0.1161)	3.1303 (0.5362)	0.0109 (0.0001)	0.3691 (0.3033)	2.2998 (0.5125)	0.8305 (0.3622)	1.3382 (0.5121)
JP/US	0.65 (0.9385)	0.2332 (0.1014)	2.7011 (0.6090)	622.51 (17225)	0.0385 (0.0985)	1.2270 (0.7465)	1.4741 (0.2247)	0.3288 (0.8484)
CA/US	0.99 (1.4152)	0.1599 (0.0432)	1.3904 (0.8458)	-1280.2 (24475)	1.4175 (0.7394)	1.0897 (0.7671)	0.3007 (0.5834)	0.0254 (0.9873)
FR/US	0.10 (0.0061)	0.8282 (0.1951)	3.2311 (0.5199)	0.5167 (0.0455)	0.7541 (0.2174)	2.3257 (0.5076)	0.9054 (0.3413)	0.1544 (0.9257)
GE/US	0.53 (0.6510)	0.2767 (0.1277)	4.7774 (0.3109)	441.51 (69490)	1.1513 (0.2438)	1.8802 (0.5976)	2.8972 (0.0887)	0.6221 (0.7326)
(73:I~90:II)	0.46 (0.3053)	0.3126 (0.0929)	3.5341 (0.4726)	0.3308 (0.1172)	3.8195 (2.5034)	1.9107 (0.5911)	1.6234 (0.2026)	1.8490 (0.3967)
IT/US	0.12 (0.0130)	0.7613 (0.2207)	0.3345 (0.9874)	0.0139 (0.0109)	2.2643 (1.6649)	0.2137 (0.9753)	0.1208 (0.7281)	0.1641 (0.9212)
US/UK	0.48 (0.3801)	0.3027 (0.1028)	4.0184 (0.4035)	0.4131 (0.0225)	1.1457 (0.2426)	3.2831 (0.3500)	0.7353 (0.3911)	0.1973 (0.9060)
JP/UK	0.20 (0.0472)	0.5754 (0.1715)	2.0641 (0.7239)	1129.6 (66268)	0.2187 (1.3084)	1.9893 (0.5746)	0.0748 (0.7844)	0.6517 (0.7219)
CA/UK	0.38 (0.2335)	0.3646 (0.1257)	1.7441 (0.7827)	-1.0422 (1.2608)	0.3144 (0.3579)	1.7209 (0.6322)	0.0232 (0.8789)	0.2418 (0.8861)
FR/UK	0.12 (0.0136)	0.7684 (0.2465)	2.8361 (0.5856)	0.4933 (0.1041)	0.9099 (0.5688)	2.7174 (0.4372)	0.1187 (0.7304)	0.6843 (0.7102)
GE/UK	0.61 (0.3161)	0.2457 (0.0490)	4.7501 (0.3139)	1.3017 (7.9849)	2.5730 (0.4883)	3.6556 (0.3011)	1.0945 (0.2954)	0.5691 (0.7523)
(73:I~90:II)	0.59 (2.2807)	0.2535 (0.0604)	1.7401 (0.7834)	-0.0218 (0.0083)	-0.0191 (0.0267)	1.4433 (0.6954)	0.2968 (0.5858)	0.8239 (0.6623)
IT/UK	0.43 (0.3610)	0.3289 (0.1322)	5.5458 (0.2357)	0.3795 (0.2001)	1.0832 (0.4262)	3.9265 (0.2695)	1.6193 (0.2031)	3.8965 (0.1425)

Note: For the unrestricted estimation,  $b_{u,hs}$  is the estimate for the speed of adjustment coefficient from the Hansen and Sargent equations, and  $b_{u,ga}$  is the estimate for the coefficient obtained from the price adjustment equation.

Column (a): Half-life in years.

Column (a), (b), (d) and (e): Standard errors are in parenthesis.

Column (c), (f), (g), and (h): P-values are in parenthesis.



**Table 3. The System Method Results for PPI-based Real Exchange Rates**

<b>Currencies</b>	<b>Half-life (a)</b>	<b><math>b_r</math> (b)</b>	<b><math>J_r</math> (c)</b>	<b><math>b_{u,hs}</math> (d)</b>	<b><math>b_{u,ga}</math> (e)</b>	<b><math>J_u</math> (f)</b>	<b>LR (g)</b>	<b>LR1 (h)</b>
US/CA	0.10 (0.0045)	0.8283 (0.1449)	3.1364 (0.5352)	0.5114 (0.8777)	0.8212 (0.1642)	2.9511 (0.3992)	0.1853 (0.6668)	0.6545 (0.7209)
UK/CA	0.23 (0.0420)	0.5339 (0.1079)	2.5849 (0.6294)	0.3384 (0.2081)	2.7806 (1.3857)	1.5497 (0.6708)	1.0352 (0.3089)	0.1972 (0.9061)
JP/CA	0.13 (0.0169)	0.7454 (0.2511)	1.1938 (0.8791)	0.1412 (0.4599)	0.1783 (1.4478)	0.3757 (0.9451)	0.8181 (0.3657)	0.3393 (0.8439)
FR/CA	0.19 (0.0189)	0.6004 (0.0846)	2.4459 (0.6543)	0.3637 (0.0021)	0.1796 (0.0434)	2.4453 (0.4952)	0.0006 (0.9804)	0.5578 (0.7566)
GE/CA	0.19 (0.0499)	0.6071 (0.2352)	3.9237 (0.4164)	0.3658 (0.1039)	0.5451 (0.2661)	3.3889 (0.3354)	0.5348 (0.4645)	0.4599 (0.7945)
(73:I~90:II)	0.17 (0.0433)	0.6349 (0.2560)	0.1021 (0.9987)	351.37 (27572)	2.1037 (2.0078)	0.0972 (0.9921)	0.0049 (0.9441)	0.0061 (0.9969)
IT/CA	0.75 (0.7989)	0.2059 (0.0565)	3.5158 (0.4754)	0.3265 (0.1338)	0.9645 (0.5885)	1.7766 (0.6200)	1.7392 (0.1872)	0.4566 (0.7958)
US/FR	0.62 (0.0039)	0.2443 (0.0005)	1.5127 (0.8243)	0.4432 (0.0001)	0.3883 (0.0007)	1.2524 (0.7404)	0.2603 (0.6099)	0.8847 (0.6425)
UK/FR	0.11 (0.0026)	0.8004 (0.0648)	3.6716 (0.4522)	0.2242 (0.0311)	0.1009 (0.1853)	2.8518 (0.4150)	0.8198 (0.3652)	0.6160 (0.7349)
CA/FR	0.14 (0.0093)	0.6989 (0.0931)	4.2224 (0.3767)	0.1377 (0.0105)	2.7532 (0.9398)	1.7645 (0.6228)	2.4579 (0.1169)	3.2987 (0.1921)
JP/FR	0.48 (0.4434)	0.3033 (0.1208)	2.1432 (0.7094)	-0.3901 (0.7190)	127.22 (293.97)	1.2475 (0.7416)	0.8957 (0.3439)	1.5348 (0.4642)
GE/FR	0.08 (0.0033)	0.8752 (0.1721)	5.1450 (0.2727)	0.5112 (0.7792)	-4.0668 (7.6425)	2.9261 (0.4017)	2.2189 (0.1363)	2.3269 (0.3124)
(73:I~90:II)	0.08 (0.0026)	0.8864 (0.1561)	3.9876 (0.4076)	0.8204 (1.5587)	0.4413 (1.5096)	3.0440 (0.3848)	0.9436 (0.3313)	1.3531 (0.5083)
IT/FR	0.24 (0.0464)	0.5178 (0.1041)	1.6998 (0.7907)	523.14 (65593)	0.6511 (0.3211)	1.6692 (0.6437)	0.0306 (0.8611)	0.3552 (0.8372)
US/IT	0.31 (0.1258)	0.4301 (0.1291)	2.8384 (0.5852)	0.3189 (0.0112)	1.7063 (0.4175)	1.7928 (0.6164)	1.0456 (0.3065)	1.1859 (0.5526)
UK/IT	0.09 (0.0040)	0.8512 (0.1629)	3.3855 (0.4954)	0.8150 (0.4807)	1.9965 (1.3971)	1.0638 (0.7858)	2.3217 (0.1275)	0.3902 (0.8227)
CA/IT	0.09 (0.0032)	0.8575 (0.1398)	4.9664 (0.2907)	696.81 (61899)	0.2541 (0.1406)	4.1534 (0.2453)	0.8130 (0.3672)	4.0083 (0.1347)
FR/IT	0.98 (1.7330)	0.1619 (0.0551)	3.1431 (0.5341)	0.5395 (0.0068)	0.8451 (0.3644)	2.2176 (0.5284)	0.9255 (0.3360)	2.4558 (0.2929)
GE/IT	0.15 (0.0196)	0.6977 (0.1945)	0.5188 (0.9716)	-0.1207 (3.3810)	0.6956 (0.9064)	0.5167 (0.9151)	0.0021 (0.9634)	0.0801 (0.9607)
(73:I~90:II)	0.13 (0.0109)	0.7432 (0.1593)	0.9648 (0.9150)	33.671 (7745.5)	-2.0022 (7.5968)	0.0691 (0.9952)	0.8957 (0.3439)	0.5146 (0.7731)
JP/IT	0.72 (0.6756)	0.2129 (0.0535)	1.6755 (0.7951)	0.4997 (0.9985)	-1.9082 (3.1687)	0.6787 (0.8781)	0.9968 (0.3180)	0.5445 (0.7616)

Note: For the unrestricted estimation,  $b_{u,hs}$  is the estimate for the speed of adjustment coefficient from the Hansen and Sargent equations, and  $b_{u,ga}$  is the estimate for the coefficient obtained from the price adjustment equation.

Column (a): Half-life in years.

Column (a), (b), (d) and (e): Standard errors are in parenthesis.

Column (c), (f), (g), and (h): P-values are in parenthesis.

**Table 3. The System Method Results for PPI-based Real Exchange Rates**

<b>Currencies</b>	<b>Half-life</b>	<b><math>b_r</math></b>	<b><math>J_r</math></b>	<b><math>b_{u,hs}</math></b>	<b><math>b_{u,ga}</math></b>	<b><math>J_u</math></b>	<b>LR</b>	<b>LR1</b>
	<b>(a)</b>	<b>(b)</b>	<b>(c)</b>	<b>(d)</b>	<b>(e)</b>	<b>(f)</b>	<b>(g)</b>	<b>(h)</b>
US/GE	0.26	0.4893	5.4271	0.1796	2.5235	2.4944	2.9327	2.0976
(73:I~90:II)	(0.0623)	(0.1092)	(0.2462)	(0.0991)	(0.5931)	(0.4762)	(0.0868)	(0.3503)
	0.24	0.5183	5.0626	-1.1395	3.3927	4.4012	0.6614	0.2164
	(0.0549)	(0.1235)	(0.2809)	(4.0909)	(2.8308)	(0.2212)	(0.4160)	(0.3301)
UK/GE	0.18	0.6280	2.1148	0.1259	0.7416	2.0431	0.0717	1.5046
(73:I~90:II)	(0.0455)	(0.2542)	(0.7146)	(0.1271)	(0.5005)	(0.5635)	(0.7888)	(0.4712)
	0.15	0.6833	2.0224	654.06	0.1802	1.5121	0.5103	0.9025
	(0.0231)	(0.2027)	(0.7316)	(61983)	(0.4877)	(0.6794)	(0.4750)	(0.6368)
CA/GE	0.30	0.4399	2.6439	0.5332	2.4444	2.4751	0.1688	1.9474
(73:I~90:II)	(0.1272)	(0.1430)	(0.6190)	(0.2130)	(0.9530)	(0.4798)	(0.6811)	(0.3776)
	0.25	0.5019	6.7973	0.9761	2.9121	6.0932	0.7041	2.6732
	(0.0822)	(0.1606)	(0.1469)	(6.1268)	(2.3559)	(0.1071)	(0.4014)	(0.2627)
FR/GE	0.55	0.2687	3.3404	0.0561	0.1762	3.0777	0.2627	1.5551
(73:I~90:II)	(0.6163)	(0.1090)	(0.5025)	(0.0344)	(0.2603)	(0.3797)	(0.6082)	(0.4595)
	0.47	0.3064	3.4510	0.0224	0.4879	1.7541	1.6969	1.2838
	(0.4338)	(0.1226)	(0.4853)	(0.0185)	(0.7029)	(0.6249)	(0.1926)	(0.5262)
IT/GE	0.17	0.6345	2.2022	0.1875	1.7592	2.2015	0.0007	1.2005
(73:I~90:II)	(0.0725)	(0.4270)	(0.6986)	(0.1130)	(0.4367)	(0.5316)	(0.9788)	(0.5486)
	0.14	0.6925	0.6938	0.7158	0.8009	0.6155	0.0783	0.0607
	(0.0192)	(0.1824)	(0.9520)	(3.6612)	(0.1926)	(0.8928)	(0.7796)	(0.9701)
JP/GE	0.27	0.4762	2.0422	0.0461	0.8860	1.4674	0.5748	0.1699
(73:I~90:II)	(0.0380)	(0.0594)	(0.7279)	(0.0106)	(0.7989)	(0.6897)	(0.4483)	(0.9185)
	0.25	0.5036	1.0722	-0.5070	0.7206	1.0414	0.0308	0.2226
	(0.0801)	(0.1590)	(0.8986)	(13.512)	(0.3724)	(0.7912)	(0.8606)	(0.8946)

Note: For the unrestricted estimation,  $b_{u,hs}$  is the estimate for the speed of adjustment coefficient from the Hansen and Sargent equations, and  $b_{u,ga}$  is the estimate for the coefficient obtained from the price adjustment equation.

Column (a): Half-life in years.

Column (a), (b), (d) and (e): Standard errors are in parenthesis.

Column (c), (f), (g), and (h): P-values are in parenthesis.

**Table 4. The System Method Results for CPI-based Real Exchange Rates**

<b>Currencies</b>	<b>Half-life (a)</b>	<b><math>b_r</math> (b)</b>	<b><math>J_r</math> (c)</b>	<b><math>b_{u,hs}</math> (d)</b>	<b><math>b_{u,ga}</math> (e)</b>	<b><math>J_u</math> (f)</b>	<b>LR (g)</b>	<b>LR1 (h)</b>
US/JP	1.19 (3.4288)	0.1351 (0.0605)	6.1738 (0.1865)	1949.7 (64310)	3.7470 (2.1497)	5.0784 (0.1661)	1.0954 (0.2952)	3.8260 (0.1476)
UK/JP	0.82 (1.7569)	0.1896 (0.0942)	2.3271 (0.6758)	558.28 (36530)	-0.2171 (0.2369)	2.1092 (0.5501)	0.2179 (0.6406)	0.1517 (0.9269)
CA/JP	1.66 (5.5390)	0.0989 (0.0361)	7.0424 (0.1336)	0.2427 (0.3716)	0.9030 (0.7310)	6.7110 (0.0817)	0.3314 (0.5648)	5.2770 (0.0714)
FR/JP	1.29 (5.8398)	0.1258 (0.0819)	1.9740 (0.7405)	0.1624 (0.4519)	0.1558 (0.1222)	1.8241 (0.6096)	0.1499 (0.6986)	1.2650 (0.5312)
GE/JP	1.19 (17.932)	0.1356 (0.3202)	5.3413 (0.2540)	0.3028 (0.1936)	0.0102 (0.3029)	4.5505 (0.2078)	0.7908 (0.3738)	3.5360 (0.1706)
(73:I~90:II)	1.36 (9.3155)	0.1199 (0.1120)	2.8838 (0.5774)	0.2248 (0.1286)	1.3528 (0.5503)	2.4896 (0.4771)	0.3942 (0.5301)	0.5485 (0.7601)
IT/JP	0.76 (2.1676)	0.2027 (0.1998)	1.8546 (0.7624)	-0.1865 (0.1547)	0.6647 (0.1265)	1.0068 (0.7996)	0.8478 (0.3571)	1.2603 (0.5325)
JP/US	1.16 (3.0318)	0.1383 (0.0577)	2.8681 (0.5801)	0.0899 (0.0105)	1.2967 (1.1205)	1.0057 (0.7998)	1.8624 (0.1723)	1.1122 (0.5734)
UK/US	1.04 (1.6176)	0.1535 (0.0432)	5.4605 (0.2432)	3.3169 (4.6182)	-2.7018 (3.3162)	4.2778 (0.2329)	1.1827 (0.2768)	0.6494 (0.7227)
CA/US	1.38 (5.6261)	0.1179 (0.0641)	1.0369 (0.9042)	1.1506 (1.5315)	1.1020 (0.3963)	1.0238 (0.7954)	0.0131 (0.9088)	0.7055 (0.7027)
FR/US	1.57 (9.2533)	0.1045 (0.0718)	0.7785 (0.9413)	0.1020 (0.1853)	1.1107 (0.6502)	0.6121 (0.8936)	0.1664 (0.6833)	0.4167 (0.8119)
GE/US	1.57 (5.2483)	0.1044 (0.0406)	2.1670 (0.7051)	0.0479 (0.0378)	0.0551 (0.2605)	2.1317 (0.5455)	0.0353 (0.8509)	1.3882 (0.4995)
(73:I~90:II)	0.94 (1.9142)	0.1682 (0.0690)	1.9856 (0.7384)	-2584.3 (16723)	-0.2940 (0.9954)	1.3685 (0.7129)	0.6171 (0.4321)	1.0587 (0.5889)
IT/US	0.25 (0.1342)	0.5028 (0.2643)	1.1190 (0.8912)	0.1195 (0.2691)	0.7706 (0.9636)	1.0497 (0.7892)	0.0693 (0.7923)	0.3209 (0.8517)
US/UK	2.76 (3.7913)	0.0608 (0.0054)	1.3352 (0.8553)	0.0614 (0.0059)	0.8852 (0.1942)	1.0334 (0.7931)	0.3018 (0.5827)	0.1545 (0.9256)
JP/UK	2.57 (0.0565)	0.0652 (0.0001)	4.2183 (0.3772)	0.0586 (0.0251)	0.7119 (0.7019)	2.8596 (0.4137)	1.3587 (0.2437)	2.6621 (0.2642)
CA/UK	2.57 (0.2250)	0.0653 (0.0004)	5.8054 (0.2141)	0.0744 (0.0097)	0.9760 (0.2299)	5.2874 (0.1519)	0.5180 (0.4716)	4.0009 (0.1352)
FR/UK	2.27 (0.0389)	0.0735 (0.0001)	6.1451 (0.1885)	0.0631 (0.0011)	1.2141 (0.3871)	5.4676 (0.1406)	0.6775 (0.4104)	1.2051 (0.5474)
GE/UK	2.53 (0.5932)	0.0662 (0.0011)	1.4915 (0.8281)	0.0655 (0.0003)	0.0505 (0.0444)	0.9609 (0.8107)	0.5306 (0.4663)	0.3785 (0.8275)
(73:I~90:II)	1.76 (8.66)	0.0937 (0.0476)	3.3757 (0.4970)	0.1604 (0.0266)	0.2483 (0.1455)	3.0385 (0.3857)	0.3372 (0.5614)	2.2237 (0.3289)
IT/UK	2.58 (0.2294)	0.0649 (0.0004)	3.1902 (0.5265)	3.0254 (3.5186)	0.4809 (0.6287)	2.1359 (0.5446)	1.0543 (0.3045)	1.5759 (0.4547)

Note: For the unrestricted estimation,  $b_{u,hs}$  is the estimate for the speed of adjustment coefficient from the Hansen and Sargent equations, and  $b_{u,ga}$  is the estimate for the coefficient obtained from the price adjustment equation.

Column (a): Half-life in years.

Column (a), (b), (d) and (e): Standard errors are in parenthesis.

Column (c), (f), (g), and (h): P-values are in parenthesis.

**Table 4. The System Method Results for CPI-based Real Exchange Rates**

Currencies	Half-life (a)	$b_r$ (b)	$J_r$ (c)	$b_{u,hs}$ (d)	$b_{u,ga}$ (e)	$J_u$ (f)	LR (g)	LR1 (h)
US/CA	2.95 (9.3785)	0.0571 (0.0110)	2.0478 (0.7269)	0.5779 (1.8963)	4.5191 (3.1983)	0.6652 (0.8813)	1.3826 (0.2396)	0.2479 (0.8834)
UK/CA	2.57 (7.7260)	0.0651 (0.0136)	1.8403 (0.7651)	9.9071 (74.773)	3.9390 (2.6286)	0.9687 (0.8088)	0.8716 (0.3505)	1.1620 (0.5593)
JP/CA	0.40 (0.3965)	0.3528 (0.1885)	3.6762 (0.4515)	0.1878 (102.94)	0.0677 (1.8868)	3.2073 (0.3607)	0.4689 (0.4934)	0.6533 (0.7213)
FR/CA	1.15 (0.8961)	0.1399 (0.0177)	1.4873 (0.8288)	0.0171 (0.2096)	22.087 (17.522)	1.4843 (0.6858)	0.0030 (0.9563)	1.0344 (0.5961)
GE/CA	1.06 (1.5327)	0.1504 (0.0383)	2.1491 (0.7083)	0.0657 (0.4728)	15.2830 (14.210)	1.4444 (0.6951)	0.7047 (0.4012)	1.4612 (0.4816)
(73:I~90:II)	1.00 (1.7623)	0.1589 (0.0525)	3.3144 (0.5066)	0.2914 (0.3000)	13.317 (3.1861)	1.8195 (0.6106)	1.4949 (0.2214)	2.7262 (0.2558)
IT/CA	1.02 (1.3966)	0.1567 (0.0399)	2.4382 (0.6557)	-3.0380 (287.22)	1.1590 (2.4265)	1.3424 (0.7190)	1.0958 (0.2951)	0.4620 (0.7937)
US/FR	0.95 (2.3143)	0.1672 (0.0818)	1.4751 (0.8310)	0.2897 (0.0013)	0.6899 (1.8124)	0.0188 (0.9993)	1.4563 (0.2275)	0.1627 (0.9218)
UK/FR	0.21 (0.0634)	0.5574 (0.1983)	3.5303 (0.4732)	0.1749 (0.1295)	0.8604 (0.2260)	1.8452 (0.6051)	1.6851 (0.1942)	0.1647 (0.9209)
CA/FR	0.20 (0.1149)	0.5786 (0.4282)	3.7024 (0.4477)	0.1716 (0.1301)	0.8056 (0.3449)	2.3339 (0.5061)	1.3685 (0.2420)	0.1306 (0.9367)
JP/FR	2.33 (6.1011)	0.0717 (0.0145)	6.9931 (0.1362)	0.5252 (5.9762)	1.0896 (1.3579)	5.2276 (0.1558)	1.7655 (0.1839)	3.2547 (0.1964)
GE/FR	0.37 (0.2527)	0.3766 (0.1539)	4.4322 (0.3506)	0.7958 (0.3533)	0.7497 (0.2773)	4.4180 (0.2197)	0.0142 (0.9051)	1.8734 (0.3919)
(73:I~90:II)	0.41 (0.4062)	0.3412 (0.1704)	3.8233 (0.4304)	0.4274 (0.8129)	-0.1016 (1.0753)	2.6823 (0.4432)	1.1410 (0.2854)	1.3258 (0.5153)
IT/FR	0.77 (12.669)	0.2024 (0.8456)	0.8198 (0.9357)	2.5119 (2973.3)	3.7747 (4.5792)	0.7964 (0.8503)	0.0234 (0.8784)	0.1417 (0.9316)
US/IT	1.45 (8.0557)	0.1128 (0.0797)	1.3408 (0.8544)	0.0418 (0.0226)	1.3105 (0.7266)	1.3105 (0.7266)	0.0303 (0.8618)	0.1248 (0.9395)
UK/IT	0.49 (0.4920)	0.3036 (0.1345)	2.6693 (0.6145)	0.2762 (0.7971)	0.6739 (0.5354)	2.2634 (0.5195)	0.4056 (0.5242)	1.1864 (0.5525)
CA/IT	0.93 (2.3343)	0.1692 (0.0858)	3.1206 (0.5378)	1.8198 (3.8271)	0.1591 (0.2528)	2.6676 (0.4457)	0.4530 (0.5009)	0.6539 (0.7211)
FR/IT	1.09 (3.4976)	0.1462 (0.0797)	2.1628 (0.7058)	-0.0585 (0.0075)	-47.687 (54.134)	0.3665 (0.9470)	1.7963 (0.1801)	0.6956 (0.7062)
GE/IT	0.69 (1.2414)	0.2225 (0.1142)	6.2024 (0.1845)	1.6433 (9.3041)	0.7546 (0.4395)	3.7277 (0.2923)	2.4747 (0.1156)	3.7191 (0.1557)
(73:I~90:II)	0.53 (1.0483)	0.2789 (0.2115)	1.2579 (0.8684)	0.8764 (3.1149)	0.7210 (0.2140)	0.4320 (0.9335)	0.8259 (0.3634)	0.9309 (0.6278)
JP/IT	0.98 (0.8842)	0.1624 (0.0284)	5.7687 (0.2171)	0.0792 (0.0319)	0.6338 (1.2526)	4.1081 (0.2500)	1.6606 (0.1975)	3.8883 (0.1431)

Note: For the unrestricted estimation,  $b_{u,hs}$  is the estimate for the speed of adjustment coefficient from the Hansen and Sargent equations, and  $b_{u,ga}$  is the estimate for the coefficient obtained from the price adjustment equation.

Column (a): Half-life in years.

Column (a), (b), (d) and (e): Standard errors are in parenthesis.

Column (c), (f), (g), and (h): P-values are in parenthesis.

**Table 4. The System Method Results for CPI-based Real Exchange Rates**

<b>Currencies</b>	<b>Half-life (a)</b>	<b><math>b_r</math> (b)</b>	<b><math>J_r</math> (c)</b>	<b><math>b_{u,hs}</math> (d)</b>	<b><math>b_{u,ga}</math> (e)</b>	<b><math>J_u</math> (f)</b>	<b>LR (g)</b>	<b>LR1 (h)</b>
US/GE	1.09 (3.1887)	0.1469 (0.0738)	2.5382 (0.6378)	0.6637 (209.21)	1.2536 (0.6651)	1.4988 (0.6825)	1.0394 (0.3079)	0.1212 (0.9412)
(73:I~90:II)	0.80 (0.8648)	0.1945 (0.0505)	1.5798 (0.8124)	0.1641 (0.8533)	1.9877 (0.5436)	1.3786 (0.7105)	0.2012 (0.6537)	0.3480 (0.8403)
UK/GE	0.52 (0.5801)	0.2836 (0.1242)	2.0590 (0.7249)	0.6985 (18.874)	0.7204 (0.6872)	0.7304 (0.8660)	1.3286 (0.2490)	0.7843 (0.6756)
(73:I~90:II)	0.47 (0.5123)	0.3094 (0.1500)	1.9355 (0.7476)	-1.7634 (0.5604)	0.1206 (0.1036)	1.3331 (0.7213)	0.6024 (0.4376)	0.6804 (0.7116)
CA/GE	0.82 (0.6842)	0.1901 (0.0911)	4.7630 (0.3124)	0.7505 (2.8707)	1.3543 (5.1176)	2.9728 (0.3958)	1.7902 (0.1890)	2.9589 (0.2277)
(73:I~90:II)	0.70 (1.1539)	0.2201 (0.1023)	4.2978 (0.3671)	0.3512 (0.0544)	0.3559 (0.3868)	3.9716 (0.2645)	0.3262 (0.5679)	2.5822 (0.2749)
FR/GE	0.94 (1.8089)	0.1689 (0.0661)	4.7637 (0.3124)	0.1216 (0.2866)	0.4864 (0.2665)	4.4388 (0.2178)	0.3249 (0.5686)	0.4506 (0.7982)
(73:I~90:II)	0.74 (0.8484)	0.2090 (0.0631)	2.2867 (0.6831)	0.3087 (0.5935)	0.8683 (0.5818)	1.5180 (0.6781)	0.7687 (0.3806)	0.3891 (0.8232)
JP/GE	1.19 (3.4385)	0.1356 (0.0614)	0.2614 (0.9921)	0.3752 (2.6772)	-6.4276 (17.133)	0.1321 (0.9877)	0.1293 (0.7191)	0.0695 (0.9658)
(73:I~90:II)	0.80 (2.6606)	0.1947 (0.1559)	7.7267 (0.1021)	0.2025 (0.4287)	-8.4221 (29.946)	6.5928 (0.0860)	1.1339 (0.2869)	5.1531 (0.0760)
IT/GE	0.36 (0.2882)	0.3785 (0.1790)	1.3102 (0.8596)	0.9175 (3.6005)	-3.5808 (3.8845)	0.9339 (0.8172)	0.3763 (0.5395)	0.1389 (0.9329)
(73:I~90:II)	0.32 (0.1979)	0.4151 (0.1762)	2.2733 (0.6856)	0.6759 (2.8195)	-2.6007 (3.0391)	0.8772 (0.8309)	1.3961 (0.2373)	1.1734 (0.5561)

Note: For the unrestricted estimation,  $b_{u,hs}$  is the estimate for the speed of adjustment coefficient from the Hansen and Sargent equations, and  $b_{u,ga}$  is the estimate for the coefficient obtained from the price adjustment equation.

Column (a): Half-life in years; Columns (a), (b), (d) and (e): Standard errors are in parenthesis.

Column (c), (f), (g), and (h): P-values are in parenthesis.

**Table 5. The System Method Results for GDP Implicit Deflator-based Real Exchange Rates**

<b>Currencies</b>	<b>Half-life (a)</b>	<b><math>b_r</math> (b)</b>	<b><math>J_r</math> (c)</b>	<b><math>b_{u,hs}</math> (d)</b>	<b><math>b_{u,ga}</math> (e)</b>	<b><math>J_u</math> (f)</b>	<b>LR (g)</b>	<b>LR1 (h)</b>
US/JP	0.83 (2.1467)	0.1876 (0.1111)	4.9088 (0.2967)	0.4096 (0.1470)	0.0189 (0.1330)	2.2986 (0.5127)	2.6102 (0.1062)	2.9972 (0.2234)
UK/JP	0.49 (0.4096)	0.2987 (0.1056)	2.4589 (0.6520)	1.5632 (1.5698)	0.8501 (0.9983)	0.9685 (0.8088)	1.4904 (0.2221)	0.6915 (0.7076)
CA/JP	0.79 (0.8465)	0.1978 (0.0523)	0.6574 (0.9564)	1.9231 (1.0469)	6.4257 (16.015)	0.3883 (0.9426)	0.2691 (0.6039)	0.2436 (0.8853)
FR/JP	0.98 (2.9923)	0.1625 (0.0963)	3.2477 (0.5172)	2.4014 (6.9302)	0.7707 (0.4269)	2.5425 (0.4676)	0.7053 (0.4010)	0.3638 (0.8336)
GE/JP	1.20 (3.5963)	0.1344 (0.0624)	2.3715 (0.6677)	0.8161 (0.7627)	1.6872 (0.9392)	1.9147 (0.5902)	0.4568 (0.4991)	0.2595 (0.8783)
(73:I~90:II)	0.91 (1.9044)	0.1734 (0.0759)	4.0708 (0.3965)	0.1460 (0.3073)	0.7949 (0.1196)	3.8065 (0.2831)	0.2643 (0.6071)	2.2510 (0.3244)
IT/JP	0.72 (1.3384)	0.2145 (0.1087)	3.0014 (0.5575)	0.9963 (1.2445)	0.7785 (0.8298)	2.6664 (0.4459)	0.3350 (0.5627)	0.5855 (0.7462)
JP/US	0.72 (0.8143)	0.2136 (0.0652)	1.6160 (0.8058)	4558.4 (23229)	-0.3416 (0.3728)	0.7416 (0.8633)	0.8744 (0.3497)	0.3668 (0.8324)
UK/US	0.31 (0.1984)	0.4293 (0.2021)	2.6708 (0.6143)	0.6415 (0.1171)	2.1422 (0.2286)	2.0267 (0.5668)	0.6441 (0.4222)	0.2341 (0.8895)
CA/US	1.00 (1.4094)	0.1585 (0.0418)	3.2922 (0.5101)	0.7961 (0.6799)	-0.0917 (0.0945)	2.9578 (0.3981)	0.3344 (0.5630)	0.8305 (0.6601)
FR/US	0.64 (0.7105)	0.2383 (0.0827)	2.3665 (0.6686)	0.1354 (0.6180)	0.2121 (0.8073)	1.2031 (0.7522)	1.1634 (0.2807)	0.7600 (0.6838)
GE/US	0.63 (0.9572)	0.2394 (0.1132)	3.5216 (0.4745)	0.6966 (0.2931)	0.8197 (0.1449)	2.2731 (0.5176)	1.2485 (0.2638)	0.6610 (0.7185)
(73:I~90:II)	0.64 (1.3450)	0.2369 (0.1534)	0.7039 (0.9508)	0.6378 (0.3795)	0.0807 (0.0426)	0.1984 (0.9778)	0.5055 (0.4771)	0.5551 (0.7576)
IT/US	0.66 (0.7987)	0.2317 (0.0844)	3.4026 (0.4928)	6.2793 (23.570)	-1.1198 (0.8060)	3.4017 (0.3333)	0.0009 (0.9760)	1.7606 (0.4146)
US/UK	1.22 (2.4320)	0.1328 (0.0460)	3.2272 (0.5205)	3.5741 (14.744)	-0.0498 (0.0767)	1.9588 (0.5809)	1.2684 (0.2601)	1.4039 (0.4956)
JP/UK	0.24 (0.0174)	0.5112 (0.0370)	4.5418 (0.3376)	0.7061 (0.4596)	0.6281 (0.3133)	2.1117 (0.5495)	2.4301 (0.1190)	4.3503 (0.1135)
CA/UK	1.01 (1.5397)	0.1579 (0.0451)	4.2186 (0.3772)	0.5741 (18.388)	-0.0947 (0.1035)	3.7233 (0.2929)	0.4953 (0.4815)	2.5972 (0.2729)
FR/UK	0.56 (0.5422)	0.2667 (0.0934)	2.1831 (0.7021)	0.3869 (0.1728)	0.2286 (0.0907)	2.1807 (0.5357)	0.0024 (0.9609)	1.0023 (0.6058)
GE/UK	0.70 (0.4876)	0.2196 (0.0429)	4.0965 (0.3931)	0.0843 (0.2207)	0.1894 (0.1505)	3.8182 (0.2818)	0.2783 (0.5978)	0.3377 (0.8446)
(73:I~90:II)	0.58 (1.1457)	0.2575 (0.1745)	0.5743 (0.9658)	0.7230 (0.2074)	0.1140 (0.0812)	0.1789 (0.9809)	0.3954 (0.5294)	0.2470 (0.8838)
IT/UK	1.16 (3.6066)	0.1384 (0.0688)	3.3461 (0.5017)	49.497 (359.66)	0.1367 (0.7474)	2.8353 (0.4177)	0.5108 (0.4747)	0.5830 (0.7471)

Note: For the unrestricted estimation,  $b_{u,hs}$  is the estimate for the speed of adjustment coefficient from the Hansen and Sargent equations, and  $b_{u,ga}$  is the estimate for the coefficient obtained from the price adjustment equation.

Column (a): Half-life in years.

Column (a), (b), (d) and (e): Standard errors are in parenthesis.

Column (c), (f), (g), and (h): P-values are in parenthesis.

**Table 5. The System Method Results for GDP Implicit Deflator-based Real Exchange Rates**

Currencies	Half-life (a)	$b_r$ (b)	$J_r$ (c)	$b_{u,hs}$ (d)	$b_{u,ga}$ (e)	$J_u$ (f)	LR (g)	LR1 (h)
US/CA	0.19 (0.0377)	0.5932 (0.1585)	7.7061 (0.1029)	1.2448 (5.7849)	0.0798 (0.1079)	5.4003 (0.1447)	2.3058 (0.5802)	4.6131 (0.0996)
UK/CA	0.28 (0.1068)	0.4594 (0.1435)	2.4617 (0.6514)	0.3653 (0.0135)	0.4402 (0.1237)	1.7524 (0.6253)	0.7093 (0.3996)	1.2915 (0.5242)
JP/CA	0.46 (0.2963)	0.3160 (0.0937)	3.5871 (0.4647)	0.4704 (1.2658)	0.2425 (0.1231)	2.9524 (0.3990)	0.6347 (0.4256)	1.2011 (0.5485)
FR/CA	0.47 (0.0114)	0.3103 (0.0034)	6.4468 (0.1681)	0.1909 (0.3665)	-1.7359 (0.2935)	4.6651 (0.1980)	1.7817 (0.1819)	3.4263 (0.1803)
GE/CA	0.29 (0.0355)	0.4549 (0.0458)	3.0699 (0.5461)	0.0313 (0.0260)	0.1129 (0.1213)	1.1905 (0.7552)	1.8794 (0.1704)	0.1772 (0.9152)
(73:I~90:II)	0.21 (0.0666)	0.5534 (0.2014)	5.6864 (0.2238)	2.9685 (5.8580)	0.3635 (0.2524)	4.5665 (0.2064)	1.1199 (0.2899)	2.9883 (0.2244)
IT/CA	0.35 (0.1268)	0.3886 (0.0872)	7.3965 (0.1163)	2.6228 (8.8875)	0.1318 (0.1216)	4.4772 (0.2143)	2.9193 (0.0875)	4.2581 (0.1190)
US/FR	0.69 (0.9014)	0.2235 (0.0842)	4.2316 (0.3755)	0.4971 (0.4864)	0.0841 (0.0956)	4.0893 (0.2519)	0.1423 (0.7060)	1.3842 (0.5005)
UK/FR	0.16 (0.0119)	0.6578 (0.0848)	3.7001 (0.4480)	28.585 (39.607)	0.0921 (0.0664)	3.5531 (0.3139)	0.1470 (0.7014)	0.3819 (0.8261)
CA/FR	0.20 (0.0505)	0.5708 (0.1765)	0.4364 (0.9793)	0.1513 (3.8506)	0.3481 (0.9092)	0.3185 (0.9565)	0.1179 (0.7313)	0.2193 (0.8961)
JP/FR	1.48 (10.440)	0.1102 (0.0959)	1.3512 (0.8526)	1.2438 (6.1055)	1.7807 (4.4802)	1.1257 (0.7708)	0.2255 (0.6348)	0.1630 (0.9217)
GE/FR	0.47 (0.5226)	0.3085 (0.1514)	1.6911 (0.7923)	0.2132 (0.4161)	1.3447 (0.9176)	0.7821 (0.8537)	0.9090 (0.3403)	0.4307 (0.8062)
(73:I~90:II)	0.44 (0.3937)	0.3234 (0.1355)	1.1159 (0.8917)	0.1470 (0.2526)	0.0832 (0.1243)	0.4403 (0.9317)	0.6756 (0.4111)	0.8386 (0.6575)
IT/FR	0.45 (0.4797)	0.3207 (0.1601)	2.3232 (0.6765)	0.6138 (0.3933)	1.8593 (0.6632)	1.4132 (0.7024)	0.9100 (0.3401)	0.4847 (0.7847)
US/IT	0.58 (0.9204)	0.2610 (0.1452)	5.3563 (0.2526)	6.5224 (5.7945)	0.1518 (0.1821)	3.4220 (0.3310)	1.9343 (0.1642)	2.8638 (0.2388)
UK/IT	0.40 (0.1558)	0.3532 (0.0744)	3.5974 (0.4632)	5386.1 (31207)	-0.0979 (0.0956)	3.2491 (0.3547)	0.3483 (0.5551)	1.0512 (0.5912)
CA/IT	0.31 (0.2208)	0.4272 (0.2205)	0.5997 (0.9630)	6.8931 (40.799)	28.647 (55.341)	0.4336 (0.9332)	0.1661 (0.6836)	0.3933 (0.8214)
FR/IT	1.07 (0.2135)	0.1501 (0.0053)	4.4077 (0.3536)	0.1697 (19.659)	-1.2122 (0.3742)	3.7607 (0.2884)	0.6470 (0.4211)	0.1464 (0.9294)
GE/IT	0.39 (0.0846)	0.3615 (0.0441)	6.1783 (0.1862)	0.2766 (0.0714)	0.1628 (0.3104)	3.7831 (0.2858)	2.3952 (0.1217)	2.8920 (0.2355)
(73:I~90:II)	0.29 (0.1364)	0.4551 (0.1763)	3.6455 (0.4560)	0.4196 (0.3311)	-0.3916 (0.7137)	1.9275 (0.5875)	1.7180 (0.1889)	0.8720 (0.6466)
JP/IT	0.91 (6.3423)	0.1738 (0.2547)	1.7915 (0.7740)	0.0424 (0.2562)	0.6038 (0.5807)	1.5594 (0.6686)	0.2321 (0.6299)	0.3769 (0.8282)

Note: For the unrestricted estimation,  $b_{u,hs}$  is the estimate for the speed of adjustment coefficient from the Hansen and Sargent equations, and  $b_{u,ga}$  is the estimate for the coefficient obtained from the price adjustment equation.

Column (a): Half-life in years.

Column (a), (b), (d) and (e): Standard errors are in parenthesis.

Column (c), (f), (g), and (h): P-values are in parenthesis.

**Table 5. The System Method Results for GDP Implicit Deflator-based Real Exchange Rates**

<b>Currencies</b>	<b>Half-life (a)</b>	<b><math>b_r</math> (b)</b>	<b><math>J_r</math> (c)</b>	<b><math>b_{u,hs}</math> (d)</b>	<b><math>b_{u,ga}</math> (e)</b>	<b><math>J_u</math> (f)</b>	<b>LR (g)</b>	<b>LR1 (h)</b>
US/GE	0.41 (0.3278)	0.3437 (0.1413)	5.3330 (0.2548)	5.3996 (13.868)	0.5233 (0.6821)	3.0099 (0.3901)	2.3231 (0.1274)	2.6003 (0.2724)
(73:I-90:II)	0.32 (0.1197)	0.4193 (0.1110)	2.9811 (0.5609)	0.4013 (0.1263)	0.4557 (0.0647)	1.0434 (0.7907)	1.9377 (0.1639)	0.9010 (0.6373)
UK/GE	0.33 (0.1467)	0.4075 (0.1214)	2.9812 (0.5609)	0.2775 (0.0152)	0.1875 (0.0939)	2.4343 (0.4872)	0.5469 (0.4595)	0.7519 (0.6866)
(73:I-90:II)	0.27 (0.1108)	0.4701 (0.1639)	4.4270 (0.3512)	0.1773 (0.2409)	0.7623 (0.1754)	3.9573 (0.2661)	0.4697 (0.4931)	2.5680 (0.2769)
CA/GE	0.57 (1.2323)	0.2624 (0.2005)	2.0318 (0.7298)	0.2751 (0.1840)	0.1471 (0.2116)	1.2548 (0.7398)	0.7770 (0.3780)	0.5655 (0.7537)
(73:I-90:II)	0.47 (0.2549)	0.3081 (0.0735)	3.6157 (0.4605)	0.8419 (0.2916)	0.0573 (0.0596)	3.2325 (0.3571)	0.3832 (0.5358)	0.7320 (0.6935)
FR/GE	0.70 (1.3209)	0.2196 (0.1162)	1.0012 (0.9096)	1.0436 (1.8107)	-0.2978 (0.0841)	0.7588 (0.8592)	0.2424 (0.6224)	0.0001 (0.9998)
(73:I-90:II)	0.50 (0.1611)	0.2937 (0.0391)	3.6317 (0.4581)	0.1004 (0.7639)	-0.8021 (0.6220)	2.9925 (0.3927)	0.6392 (0.4240)	2.4225 (0.2978)
JP/GE	0.72 (0.0919)	0.2131 (0.0073)	2.1843 (0.7018)	0.6311 (0.0967)	0.0454 (0.0339)	1.2434 (0.7426)	0.9409 (0.3320)	1.9598 (0.3753)
(73:I-90:II)	0.63 (0.7895)	0.2398 (0.0939)	1.2737 (0.8658)	0.3349 (0.8858)	-0.1662 (0.9942)	0.8311 (0.8420)	0.4426 (0.5058)	0.5491 (0.7599)
IT/GE	0.30 (0.0318)	0.4349 (0.0342)	3.4296 (0.4886)	13.113 (33.293)	-0.7021 (0.4229)	3.4137 (0.3321)	0.0159 (0.8996)	3.1790 (0.2040)
(73:I-90:II)	0.30 (0.2385)	0.4395 (0.2671)	0.9591 (0.9159)	-2.4403 (4.2355)	2.2982 (2.3554)	0.4045 (0.9393)	0.5546 (0.4564)	0.7880 (0.6743)

Note: For the unrestricted estimation,  $b_{u,hs}$  is the estimate for the speed of adjustment coefficient from the Hansen and Sargent equations, and  $b_{u,ga}$  is the estimate for the coefficient obtained from the price adjustment equation.

Column (a): Half-life in years.

Column (a), (b), (d) and (e): Standard errors are in parenthesis.

Column (c), (f), (g), and (h): P-values are in parenthesis.